

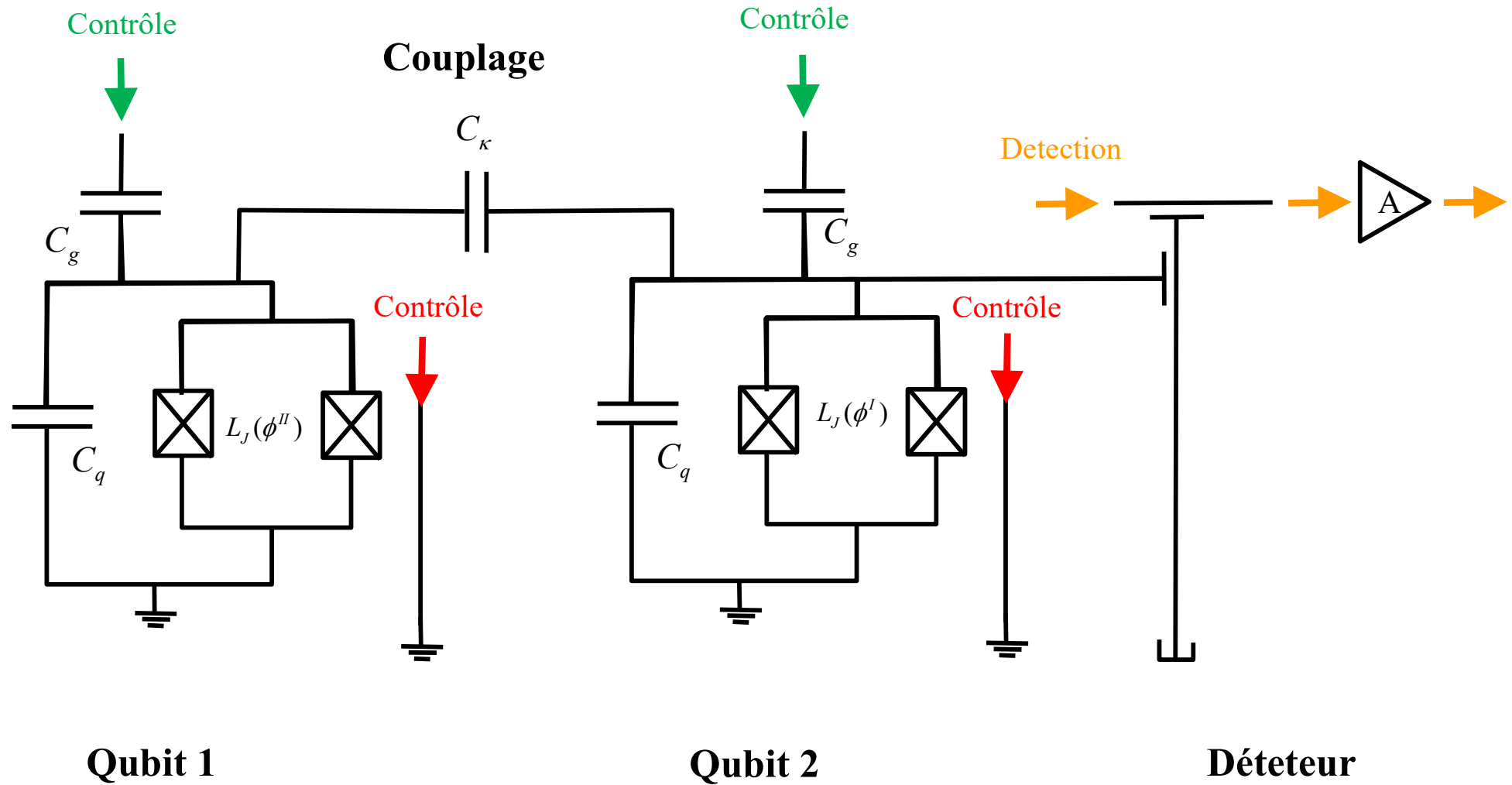
La science quantique

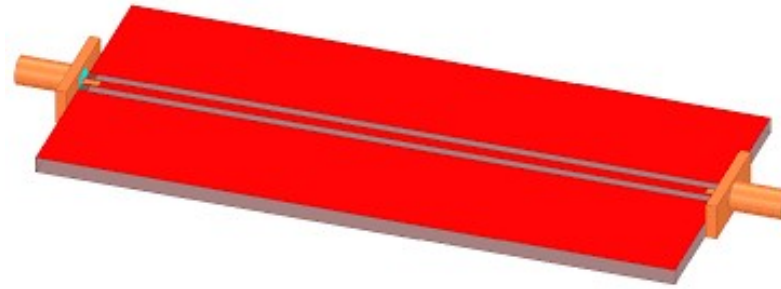
Une vision singulière

XIII) superconducting qubits

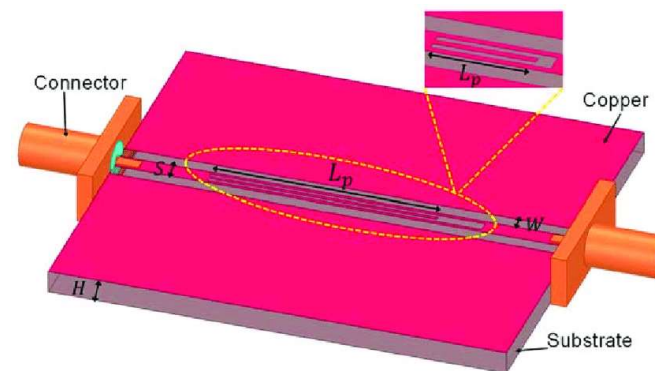
P.A. Besse

Schéma global: paire de qubits couplés



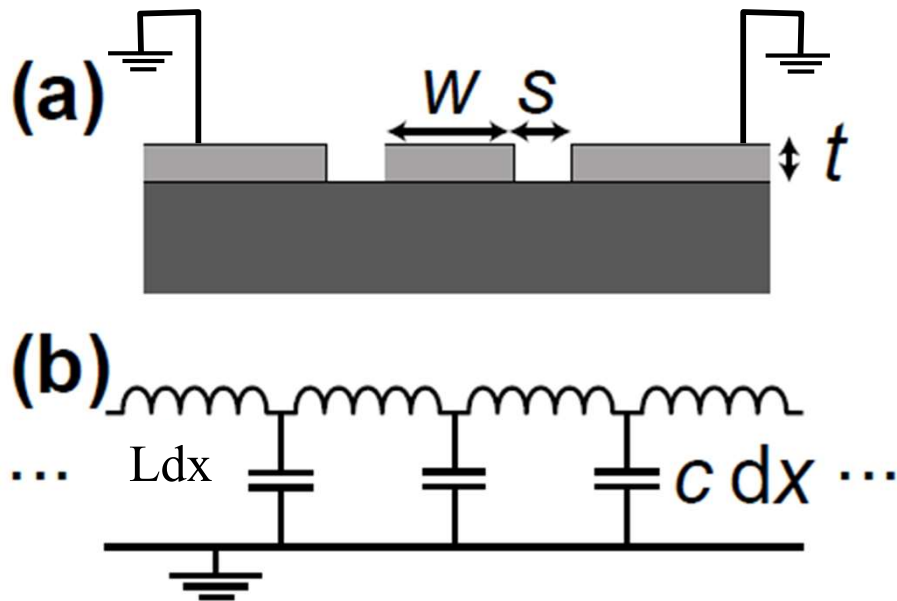


Guide d'onde coplanaire et Résonateur harmonique LC

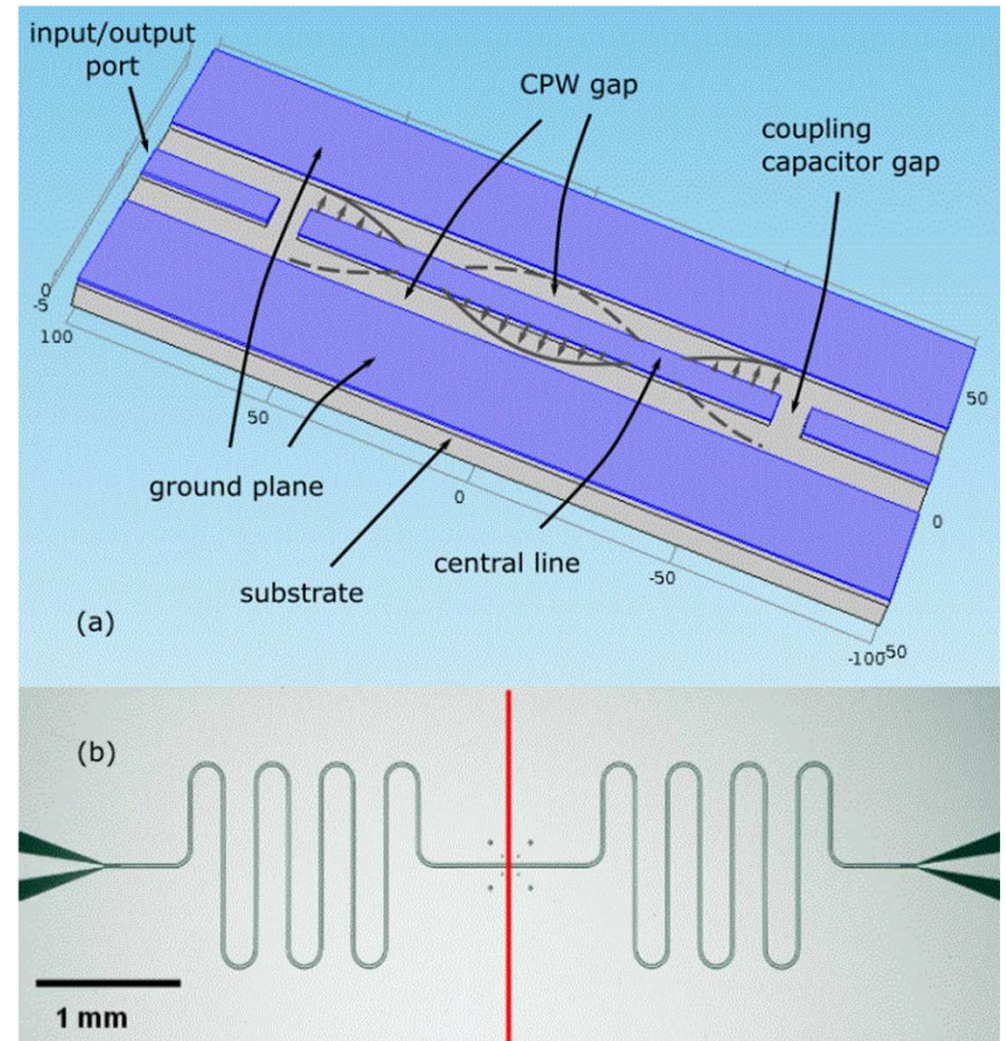


Coplanar Waveguide (CPW) Resonator

**Similaire aux câbles coaxiaux:
Résonateur LC «distribué»**

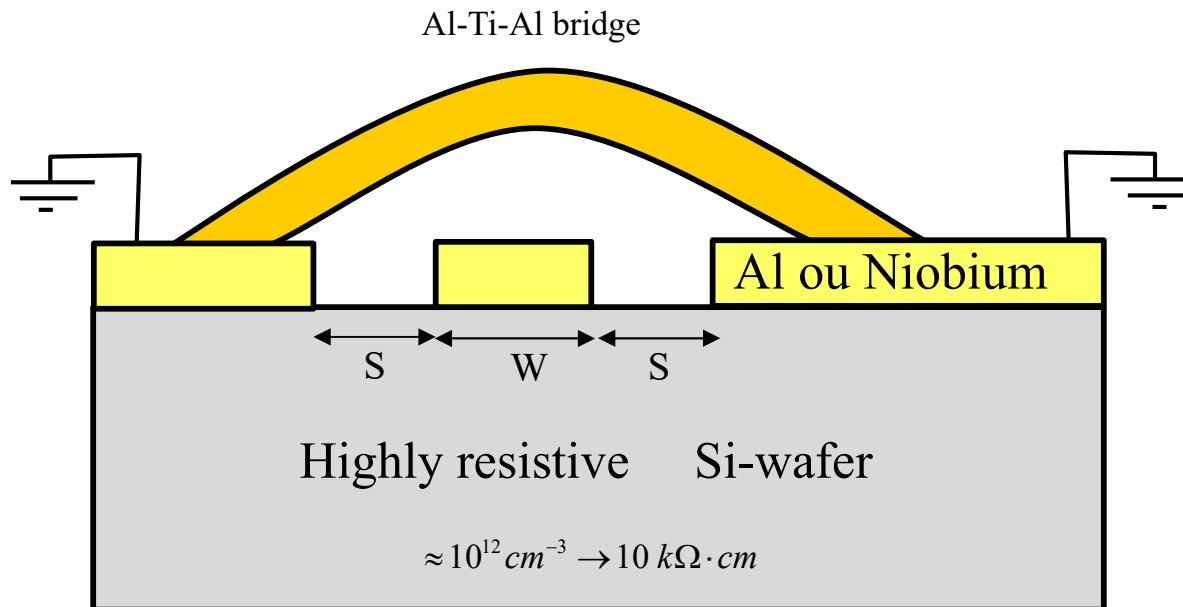


J.C Besse, ETH Thesis 27386



https://qudev.phys.ethz.ch/static/content/science/Documents/semester/Junxin_Chen_SemesterThesis_150318.pdf

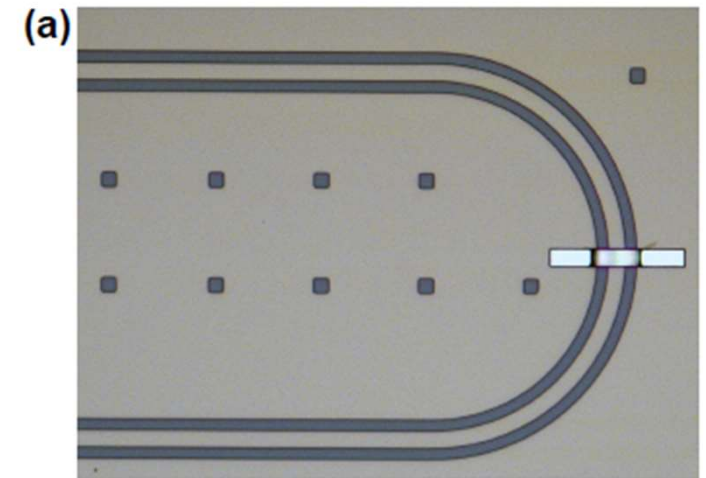
Coplanar Waveguide (CPW) Resonator



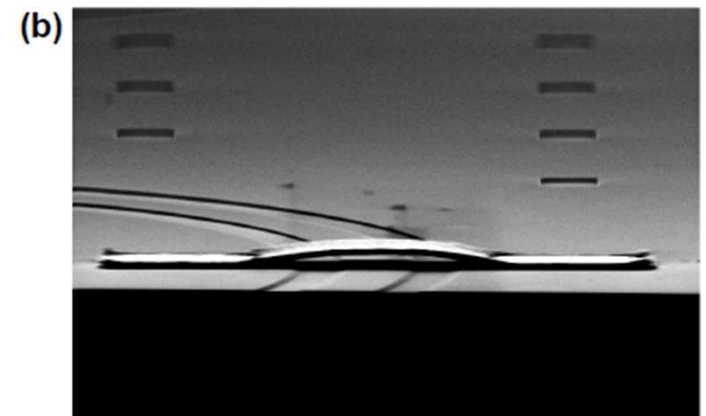
$T < 100 \text{ mK}$

$W = 10 \mu\text{m}, S = 5 \mu\text{m}$

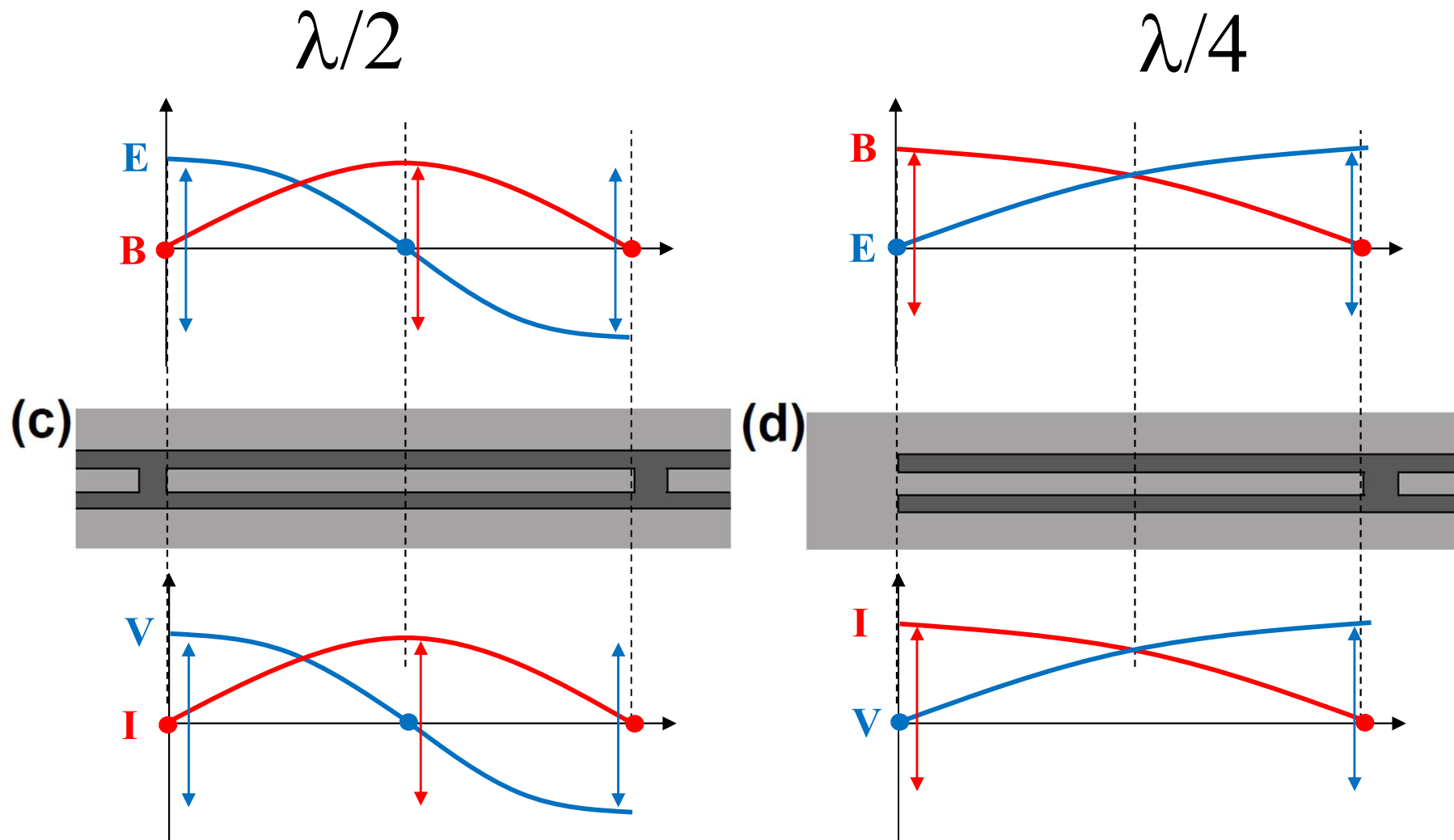
«câble coaxial»



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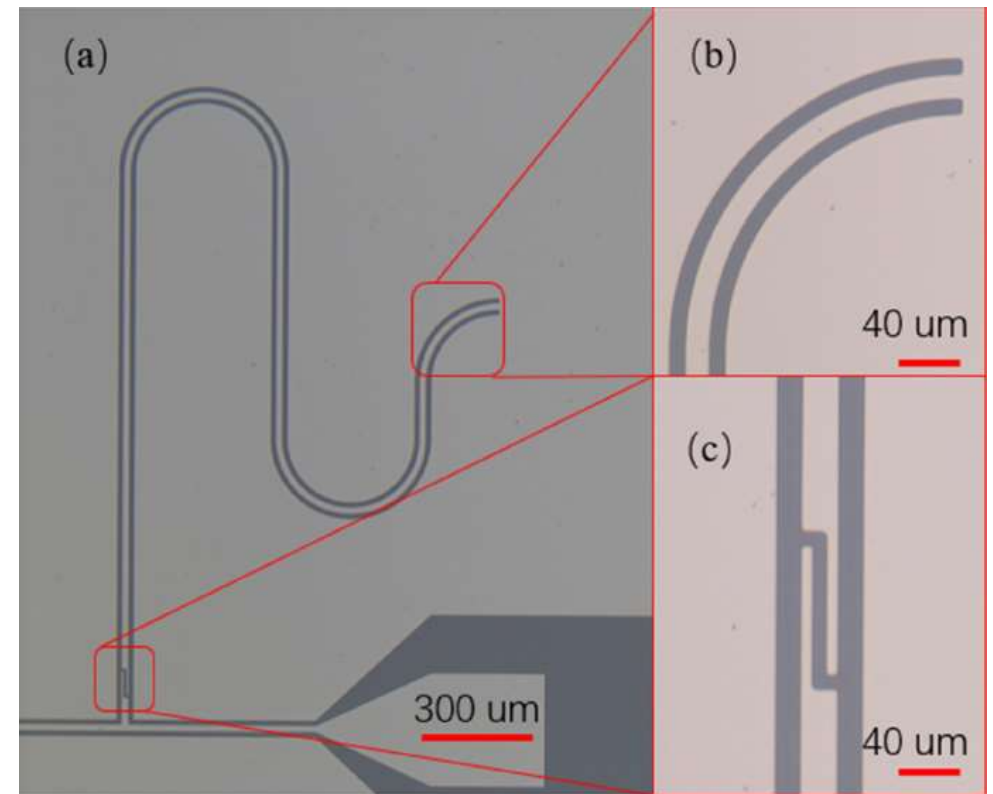
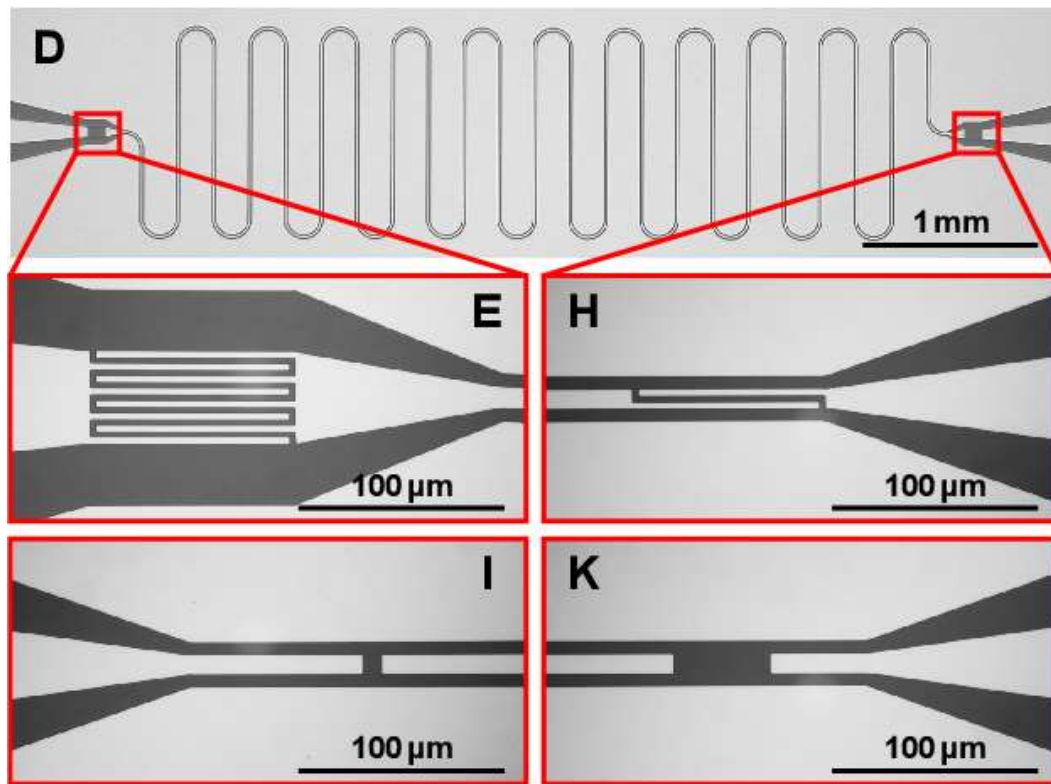


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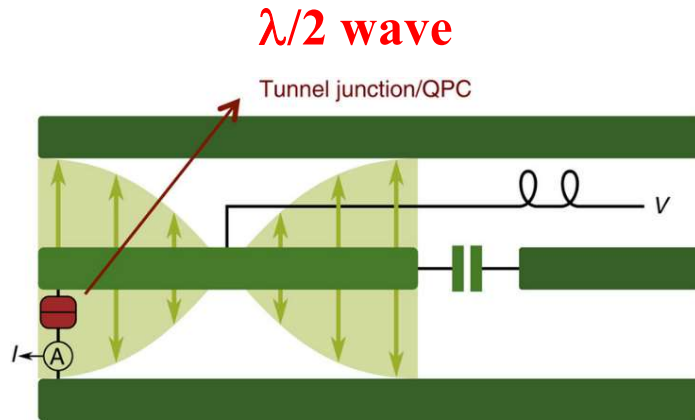
Coplanar waveguide resonator



Goppl, M. et al. “Coplanar waveguide resonators for circuit quantum electrodynamics.” *Journal of Applied Physics* 104 (2008): 113904.

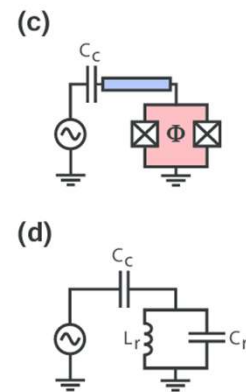
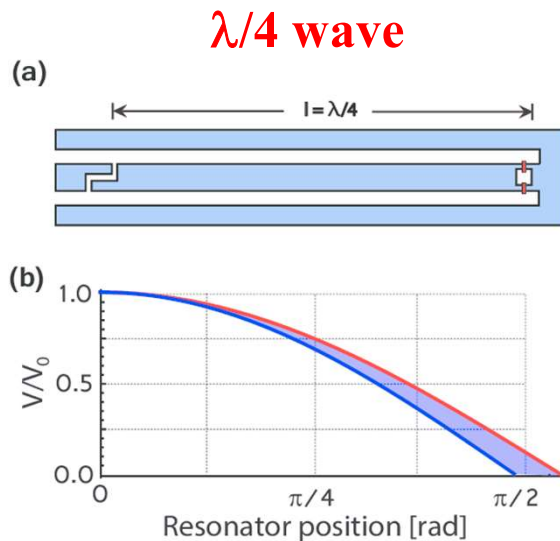
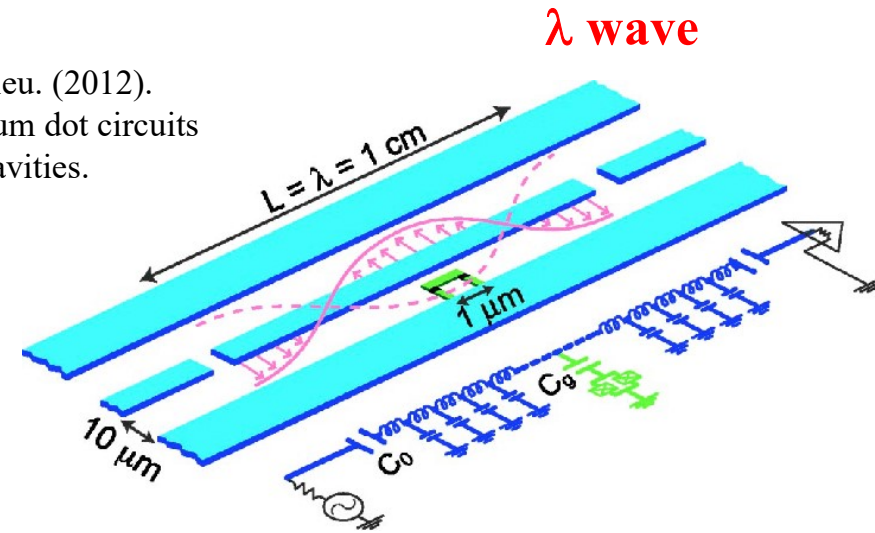
<https://link.springer.com/article/10.1007/s42452-022-04956-7>

Coplanar waveguide resonator

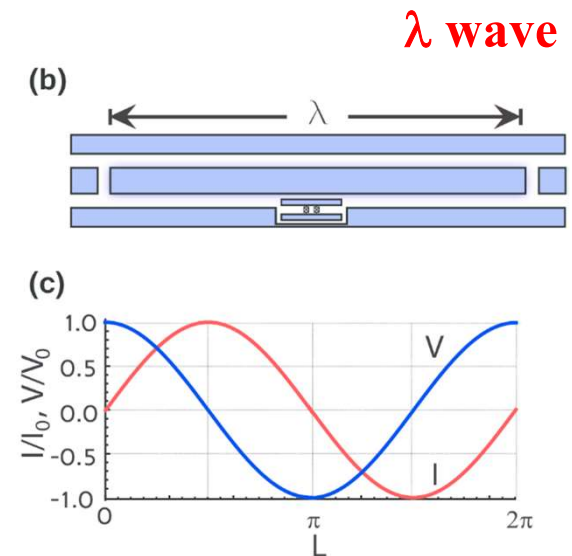


Souquet J.R. et al.. (2014). Photon-assisted tunneling with non-classical light. Nature communications. 5. 10.1038/ncomms6562.

Delbecq, Matthieu. (2012). Coupling quantum dot circuits to microwave cavities.



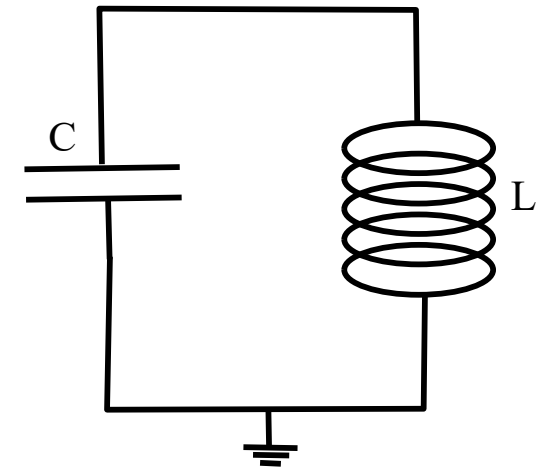
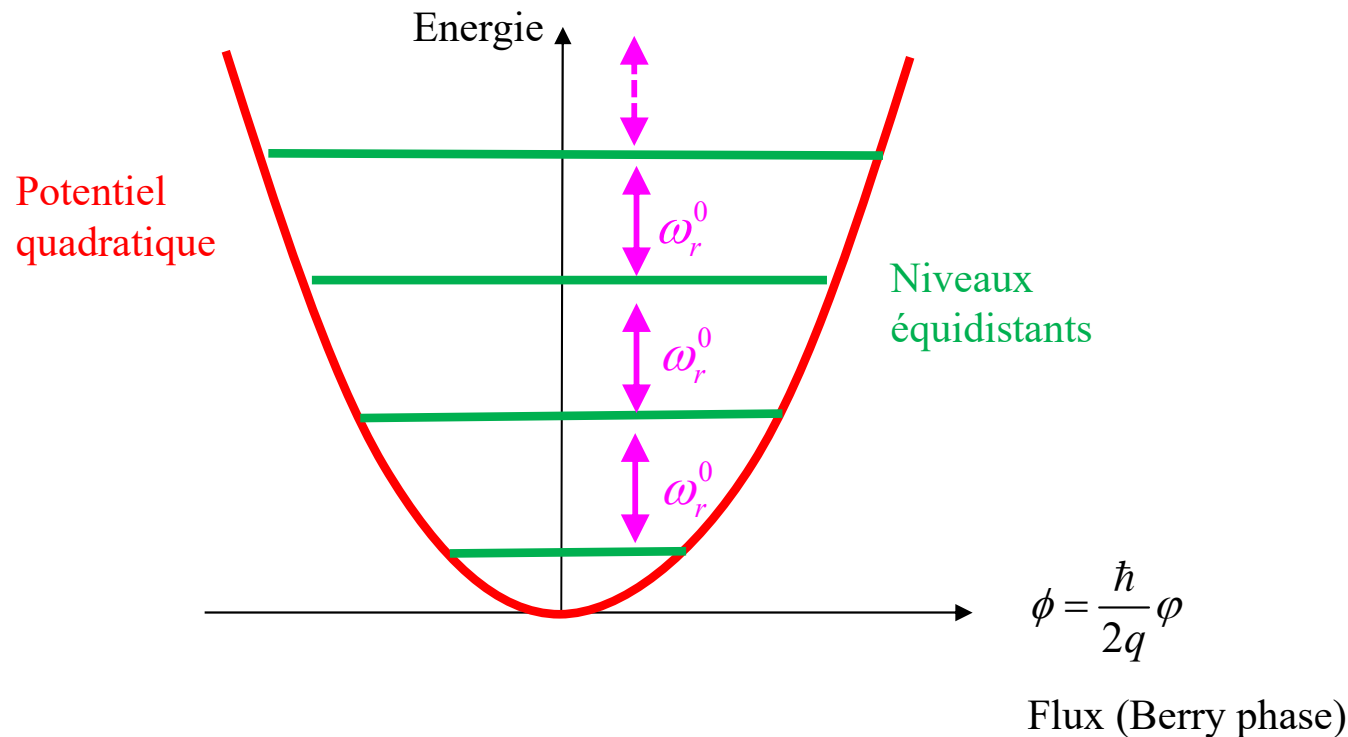
Krantz, Philip. (2013). Parametrically pumped superconducting circuits. 10.13140/RG.2.1.1071.3041.



Hamiltonien:
$$H = \underbrace{\frac{1}{2C} \cdot Q^2}_{\text{Energie capacitive}} + \underbrace{\frac{1}{2L} \cdot \phi^2}_{\text{Energie inductive}} = \hbar \omega \cdot \left(a^+ a^- + \frac{1}{2} \right)$$

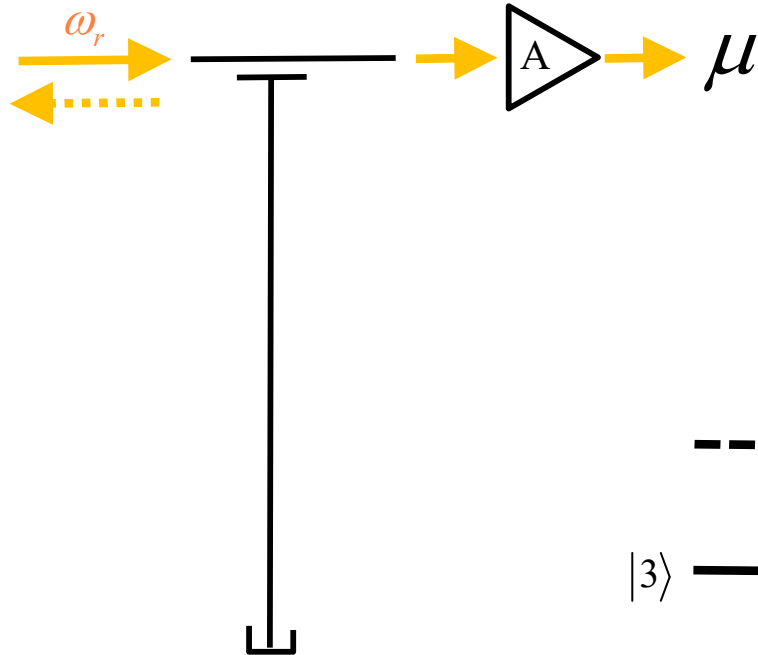
$$\omega_r \equiv \frac{1}{\sqrt{LC}}$$

Oscillateur Harmonique LC

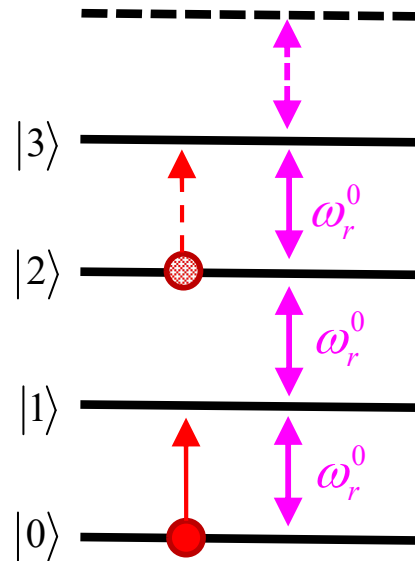


Résonateur harmonique

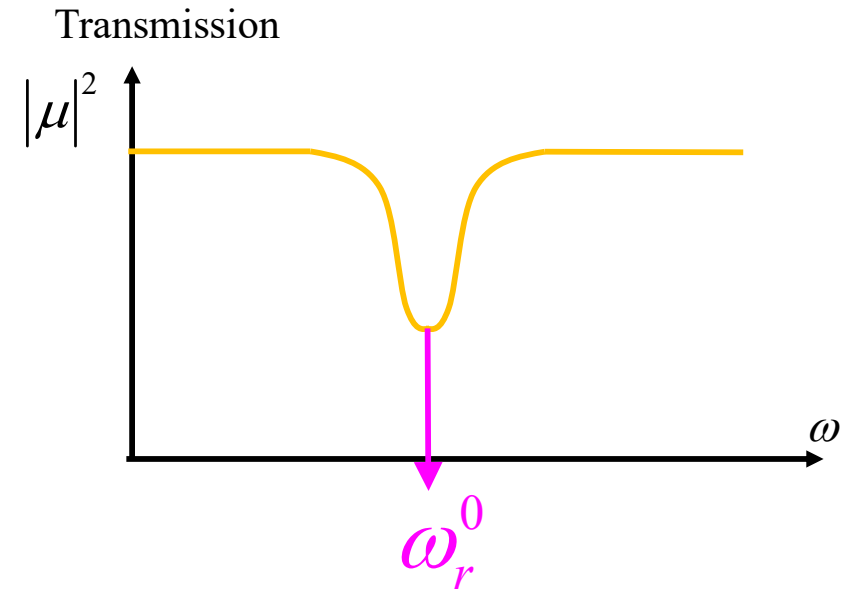
Resonator



Toutes les transitions
sont aléatoirement
possibles



Harmonic
spectrum

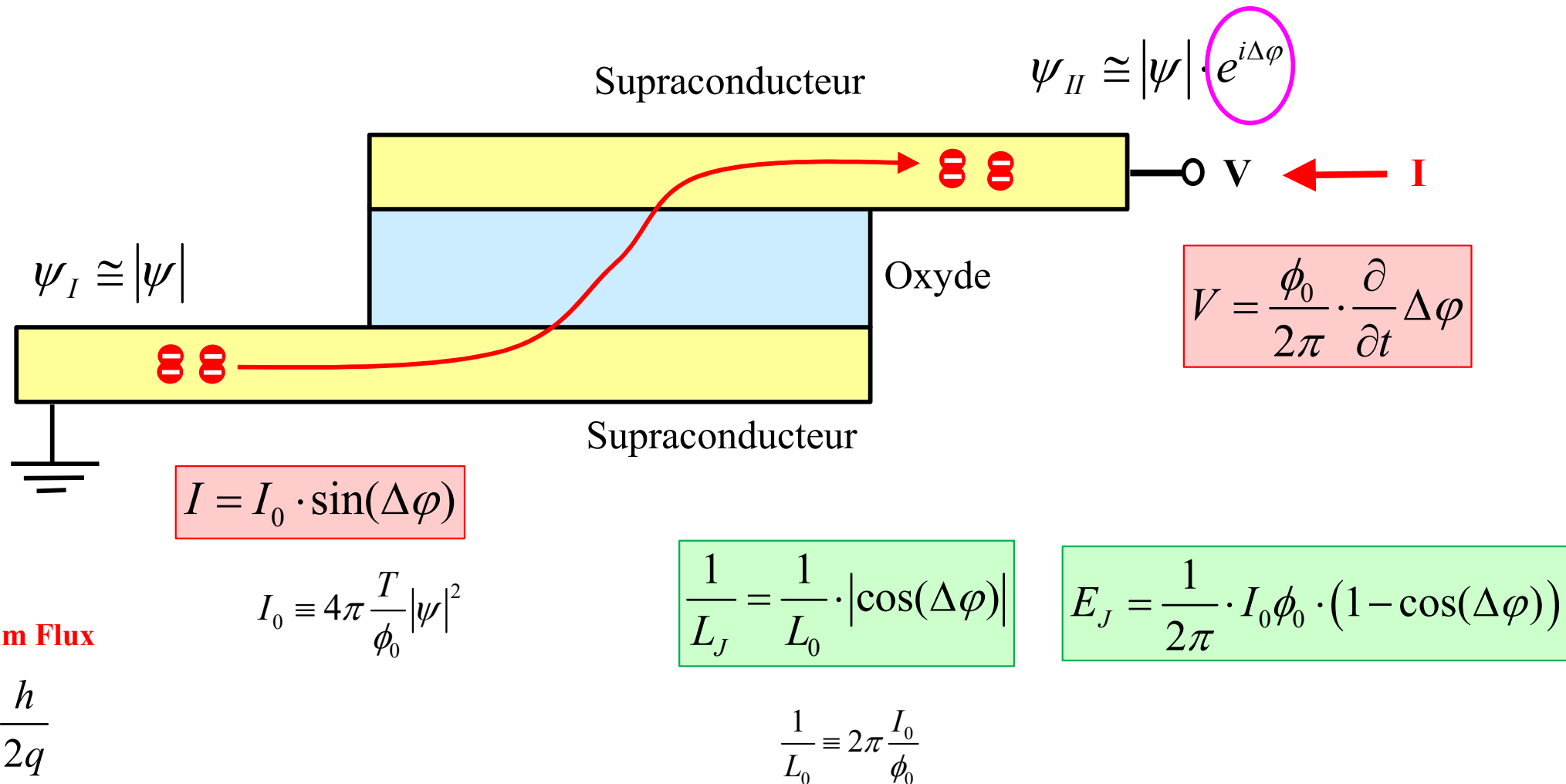


- Utilisé en sortie
comme détecteur
- Autre device nécessaire
comme qubit

Jonctions de Josephson et squids

Jonction de Josephson: résumé

Effet tunnel pour des paires de Cooper à des températures de mK.



Hamiltonien «inductif» d'une jonction de Josephson

anharmonicité

Pour une jonction de Josephson:

$$H_J \equiv E_J = \frac{1}{2\pi} I_0 \phi_0 (1 - \cos(\Delta\varphi)) \cong \frac{1}{2} \frac{1}{L_0} \cdot \left(\frac{\phi_0}{2\pi} \right)^2 \Delta\varphi^2 - O(\Delta\varphi^4)$$

Pour une bobine inductive supraconductrice:

Flux magnétique

$$H_J = \frac{1}{2} \frac{1}{L} \cdot \phi^2 = \frac{1}{2} \frac{1}{L} \cdot \left(\frac{\phi_0}{2\pi} \right)^2 \Delta\varphi^2$$

Phase de Berry:

$$\Delta\varphi = \frac{(2q)}{\hbar} \cdot \oint \vec{A} \cdot d\vec{l} = 2\pi \cdot \frac{\phi}{\phi_0}$$

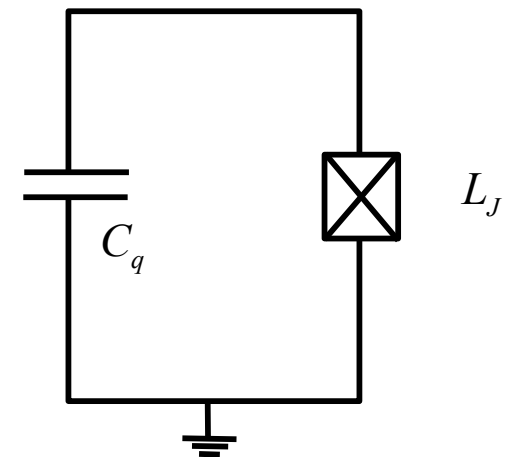
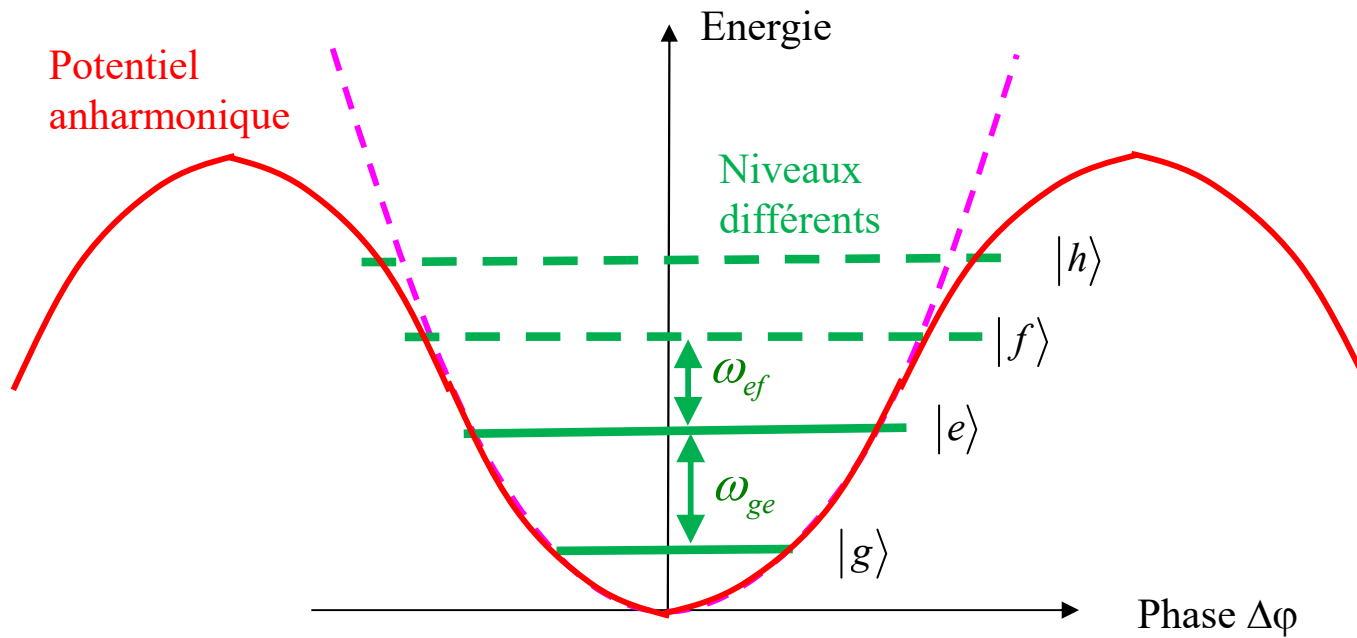
Energie
cinétique

Energie
potentielle

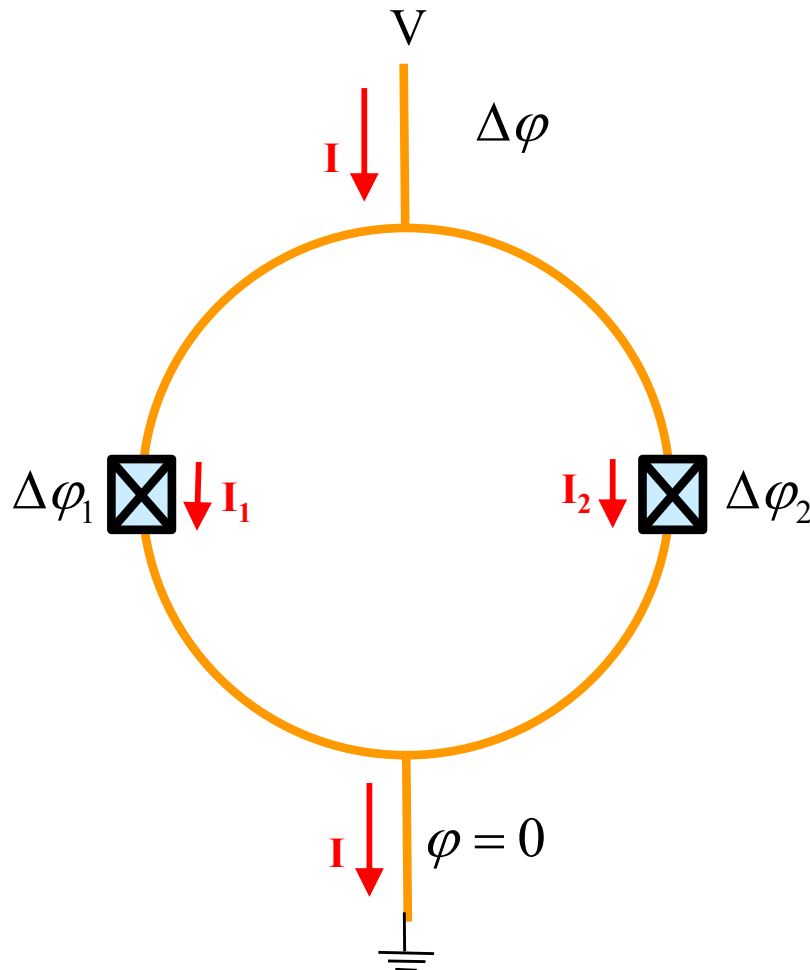
$$H = \frac{1}{2C_q} \cdot Q^2 + \frac{1}{2\pi} I_0 \phi_0 \cdot (1 - \cos(\Delta\phi)) \cong \frac{1}{2C_q} \cdot Q^2 + \frac{\phi_0}{4\pi} \cdot I_0 \cdot \Delta\phi^2 - O(\Delta\phi^4)$$

fixe

anharmonicité



Squid sans champ magnétique: deux jonctions de Josephson en parallèle



Phases

$$\Delta\varphi_1 = \Delta\varphi_2 = \Delta\varphi$$

Courants

$$I_1 = I_2$$

$$I = 2I_0 \cdot \sin(\Delta\varphi)$$

Inductance

$$\frac{1}{L_J} = \frac{1}{L_0} \cdot |\cos(\Delta\varphi)|$$

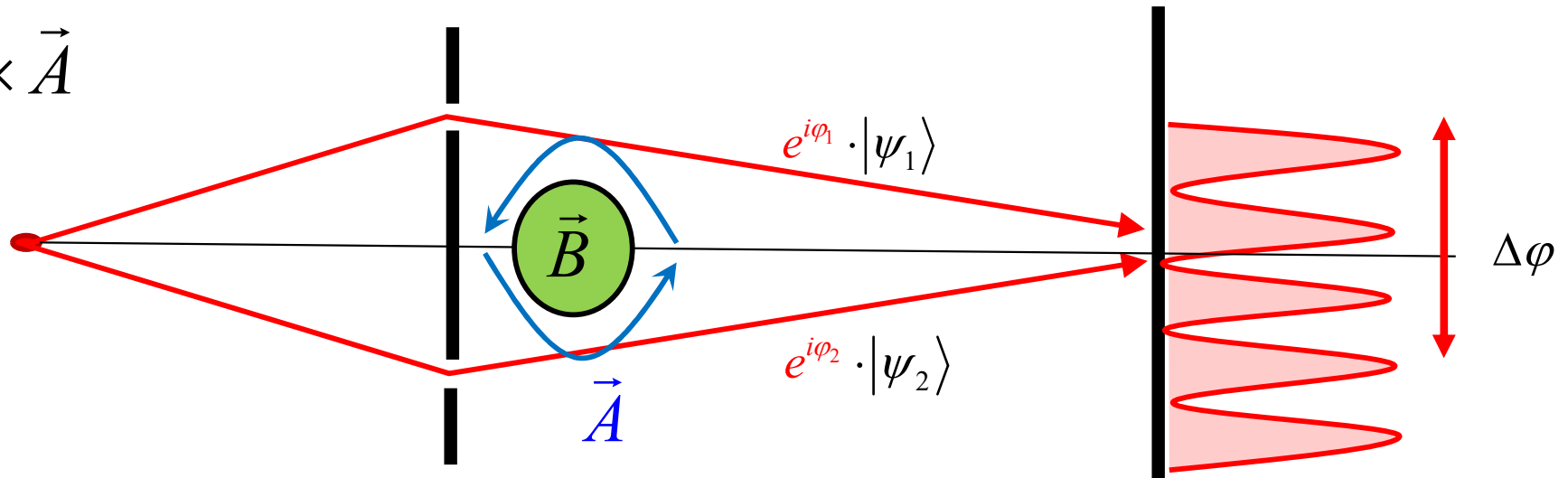
$$\frac{1}{L_0} \equiv 2\pi \frac{2I_0}{\phi_0}$$

Energie

$$E_J = \frac{1}{2\pi} \cdot 2I_0 \cdot \phi_0 \cdot (1 - \cos(\Delta\varphi))$$

Rappel: Effet Aharonov-Bohm

$$\vec{B} = \vec{\nabla} \times \vec{A}$$



Hamiltonien:

$$H = \frac{1}{2m_e} \left(\frac{\hbar}{i} \vec{\nabla} - q\vec{A} \right)^2$$

Modes propres: $e^{i\varphi_1} \cdot |\psi_1\rangle$ $e^{i\varphi_2} \cdot |\psi_2\rangle$

Phase de Berry

$$\varphi = \frac{q}{\hbar} \cdot \int_0^x \vec{A} \cdot d\vec{l}$$

$$\Delta\varphi \equiv \varphi_1 - \varphi_2 = \frac{q}{\hbar} \cdot \oint \vec{A} \cdot d\vec{l} = \frac{q}{\hbar} \cdot \iint \vec{B} \cdot d\vec{S} = 2\pi \cdot \frac{q}{h} \cdot \phi_{mag}$$

Squid avec champ magnétique

$$\sin(x - y) + \sin(x + y) = 2 \cos(y) \cdot \sin(x)$$

$$I = \tilde{I}_0(\phi) \cdot \sin(\Delta\varphi)$$

$$V = \frac{\phi_0}{2\pi} \cdot \frac{\partial}{\partial t} \Delta\varphi$$

$$\frac{1}{L_J} = \frac{1}{L_0} \cdot |\cos(\Delta\varphi)| \quad \frac{1}{L_0} \equiv 2\pi \cdot \frac{\tilde{I}_0(\phi)}{\phi_0}$$

$$E_J(\phi, \varphi) = \frac{1}{2\pi} \cdot \tilde{I}_0(\phi) \cdot \phi_0 \cdot (1 - \cos(\Delta\varphi)) \cong \frac{1}{4\pi} \cdot \tilde{I}_0(\phi) \cdot \phi_0 \cdot \Delta\varphi^2$$

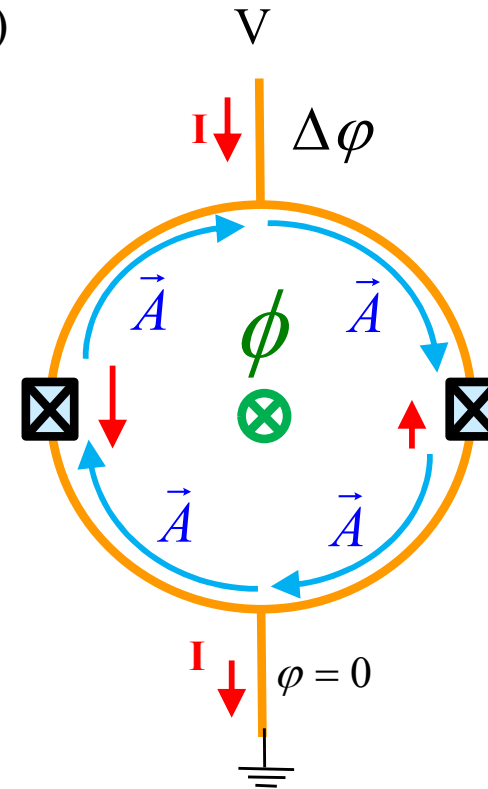
contrôlable

$$I_1 = I_0 \cdot \sin(\Delta\varphi_1)$$

$$\Delta\varphi_1 = \Delta\varphi - \pi \cdot \frac{\phi}{\phi_0}$$

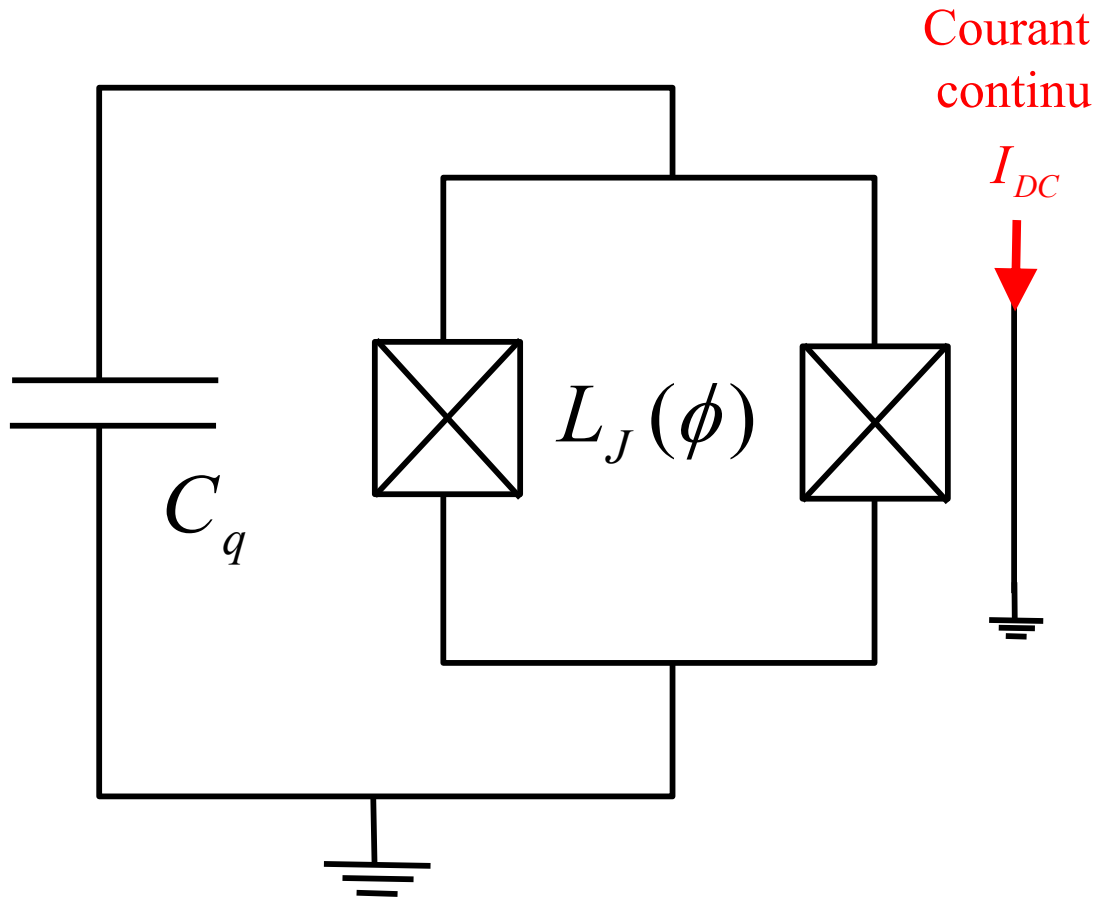
$$I_2 = I_0 \cdot \sin(\Delta\varphi_2)$$

$$\Delta\varphi_2 = \Delta\varphi + \pi \cdot \frac{\phi}{\phi_0}$$



$$\tilde{I}_0(\phi) = 2I_0 \cos\left(\pi \cdot \frac{\phi}{\phi_0}\right)$$

Résonateur anharmonique: Qubit supraconducteur



$$\frac{1}{L_J(\Delta\phi, \phi)} \equiv \frac{1}{L_0(\phi)} \cdot |\cos(\Delta\phi)|$$

$$\frac{1}{L_0(\phi)} \equiv 2\pi \frac{\tilde{I}_0(\phi)}{\phi_0}$$

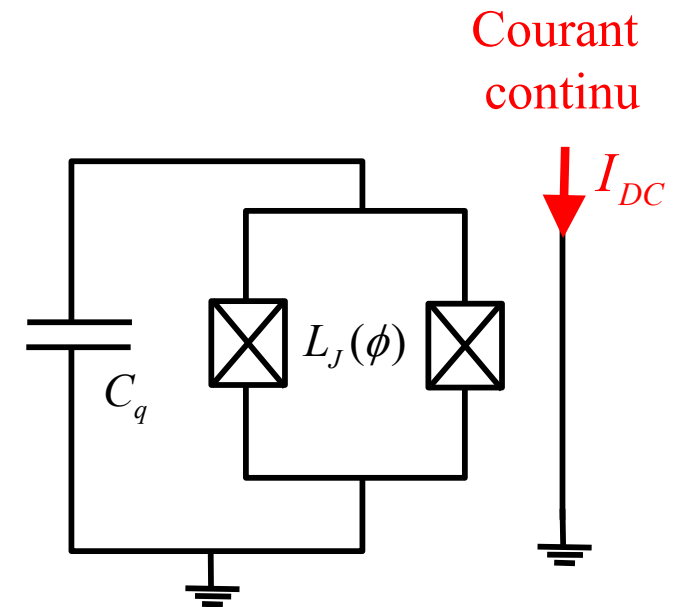
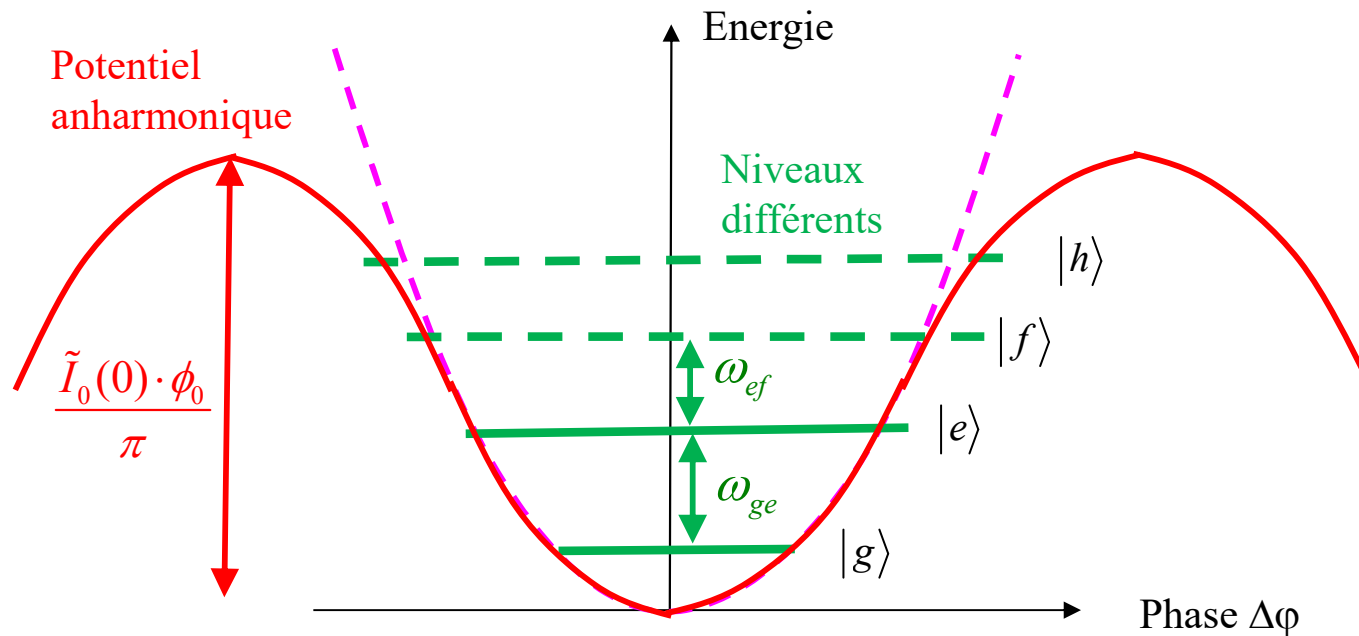
Fréquence

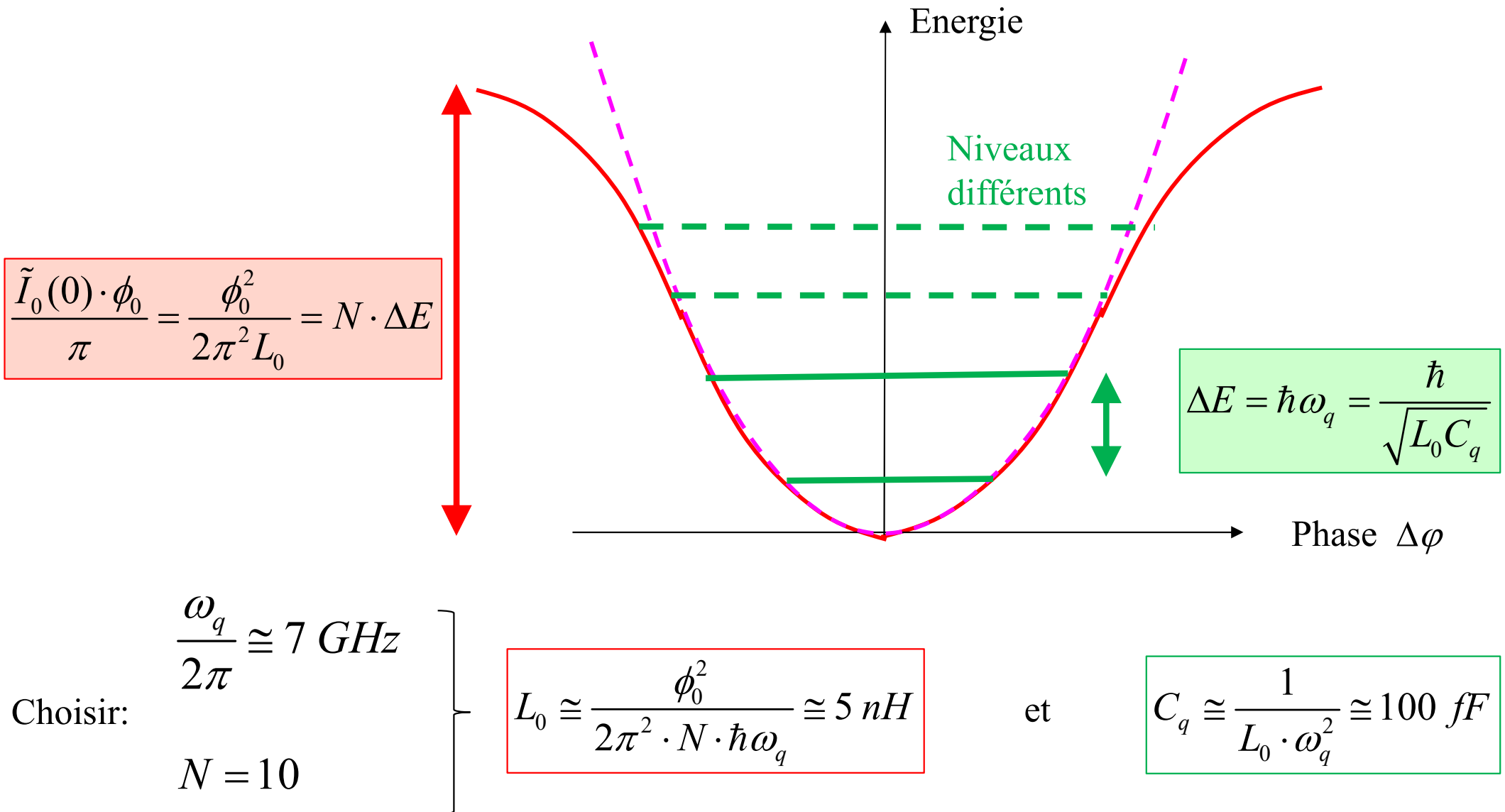
$$\omega_q(\phi) \equiv \frac{1}{\sqrt{L_0(\phi)C_q}} \approx \sqrt{\left| \cos\left(\pi \cdot \frac{\phi}{\phi_0}\right) \right|}$$

Energie
cinétique

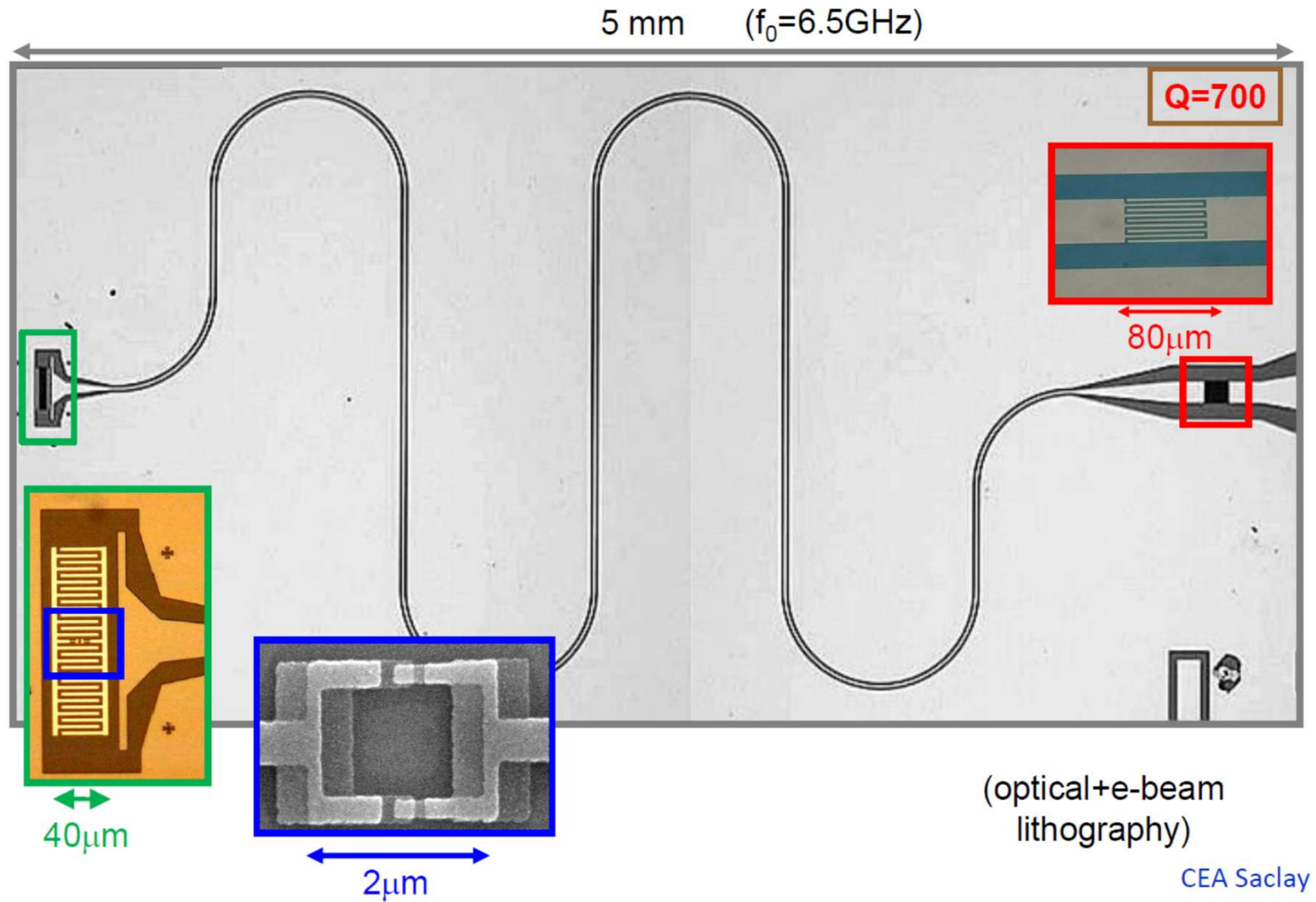
Energie
potentielle

$$H = \frac{1}{2C_q} \cdot Q^2 + \frac{\tilde{I}_0(\phi) \cdot \phi_0}{\pi} \cdot \frac{(1 - \cos(\Delta\phi))}{2} \cong \frac{1}{2C_q} \cdot Q^2 + \left(\frac{\phi_0}{4\pi} \cdot \tilde{I}_0(\phi) \right) \cdot \Delta\phi^2 - O(\Delta\phi^4)$$

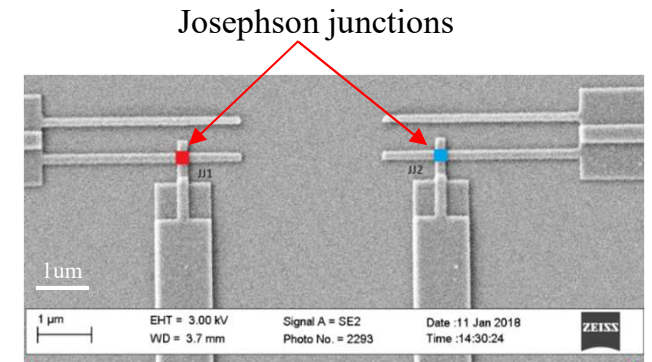
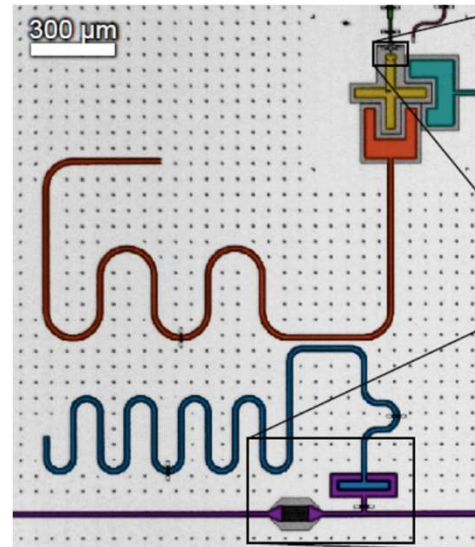
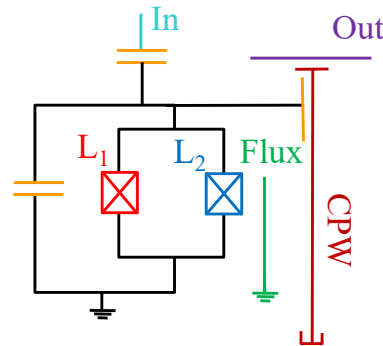
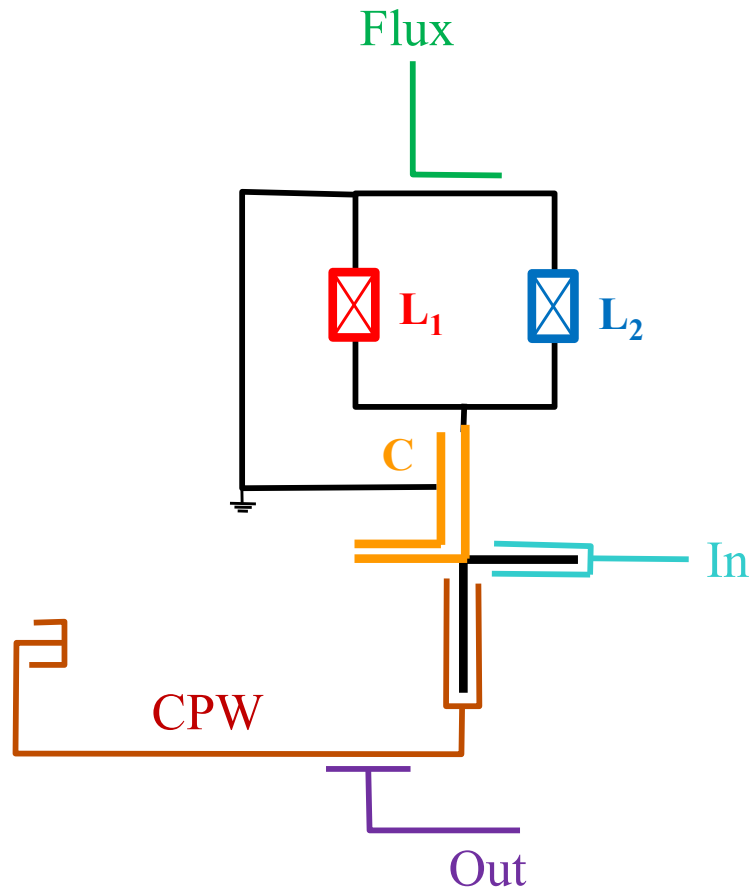




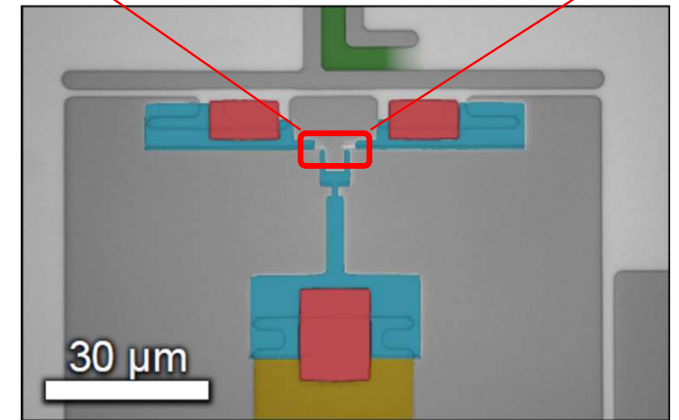
Exemples de transmons



Exemples de transmons



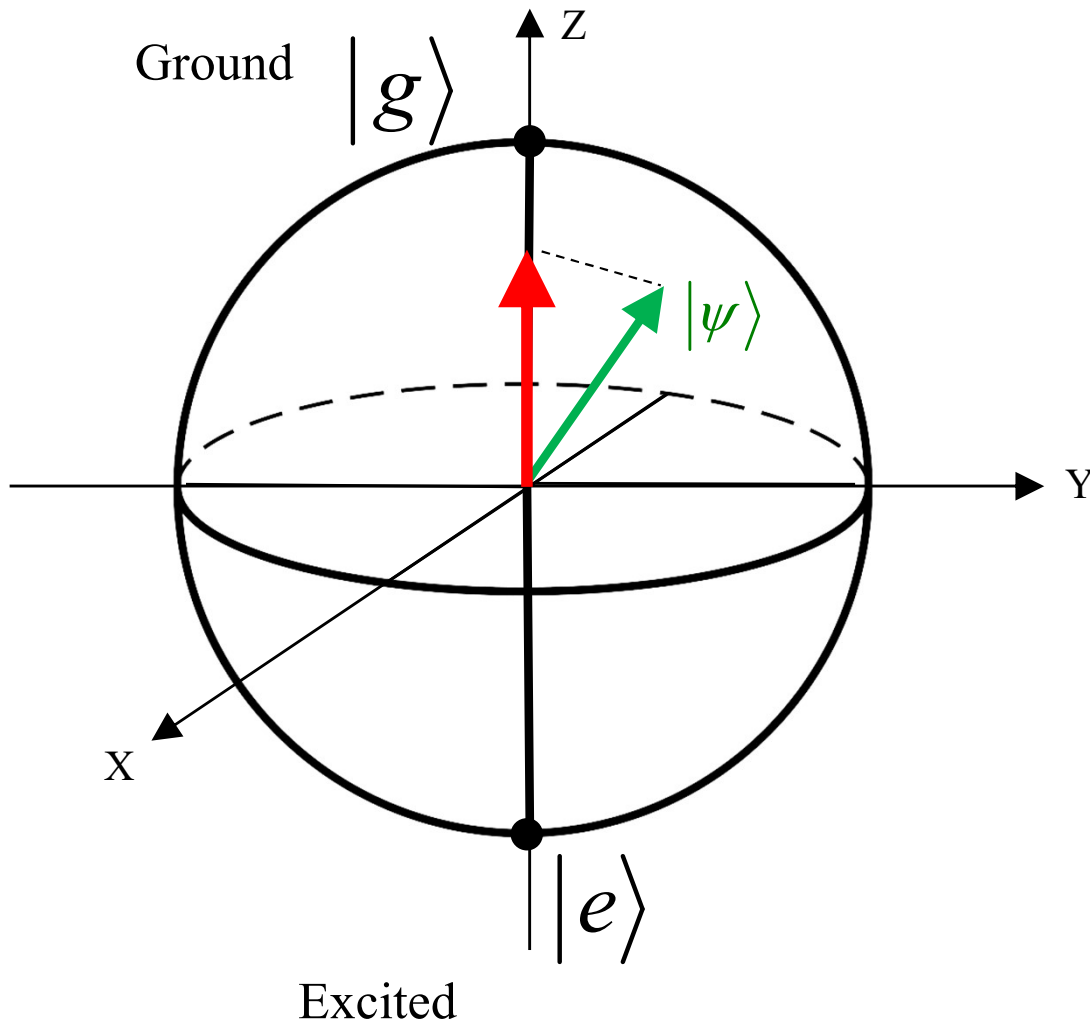
J.-C. Besse, private communication



<https://www.nature.com/articles/s41534-019-0185-4>

Couplage
avec un résonateur:

Mesures en résonnance



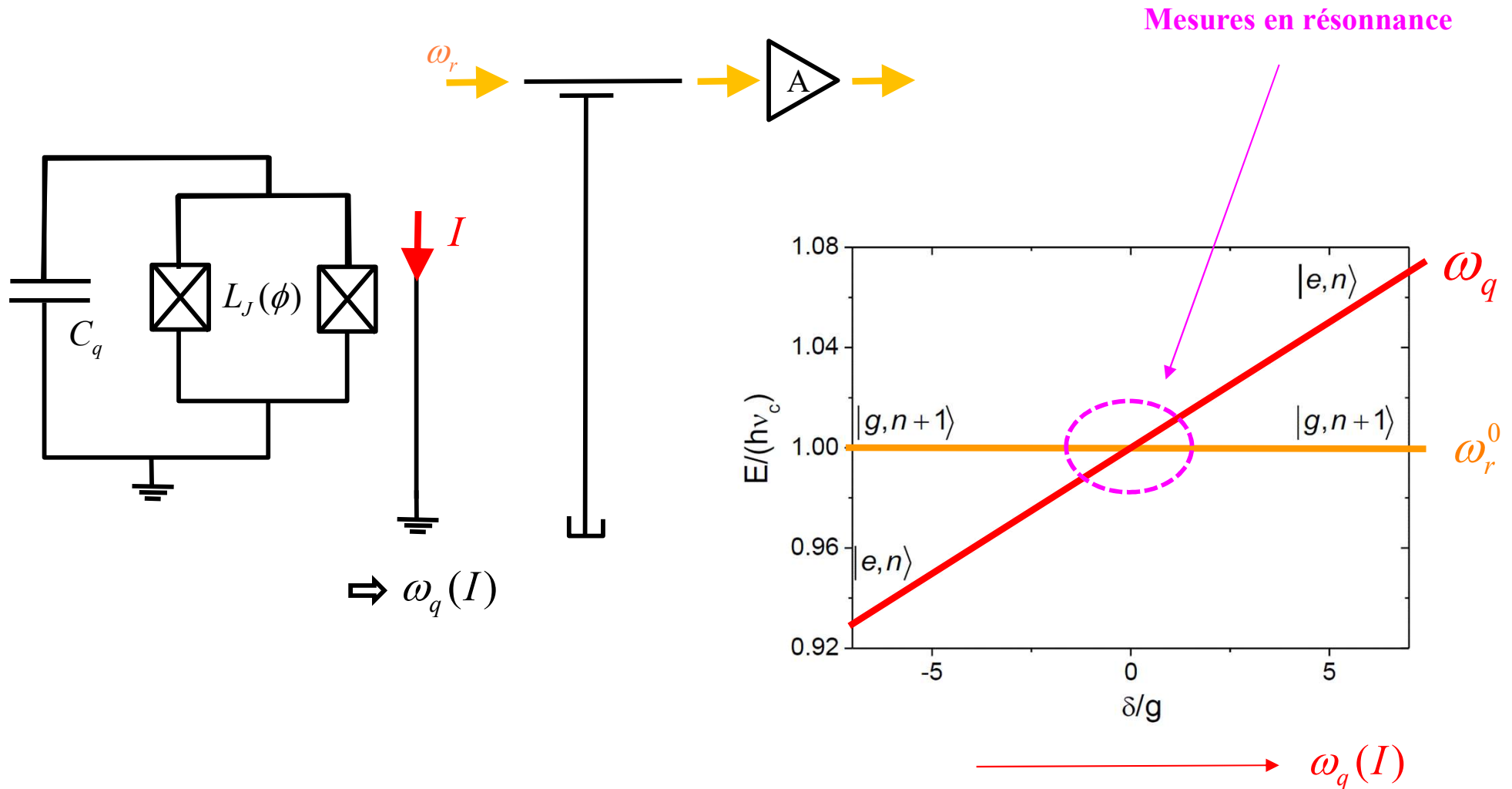
Mesures en Z

$$\langle \sigma_z \rangle$$

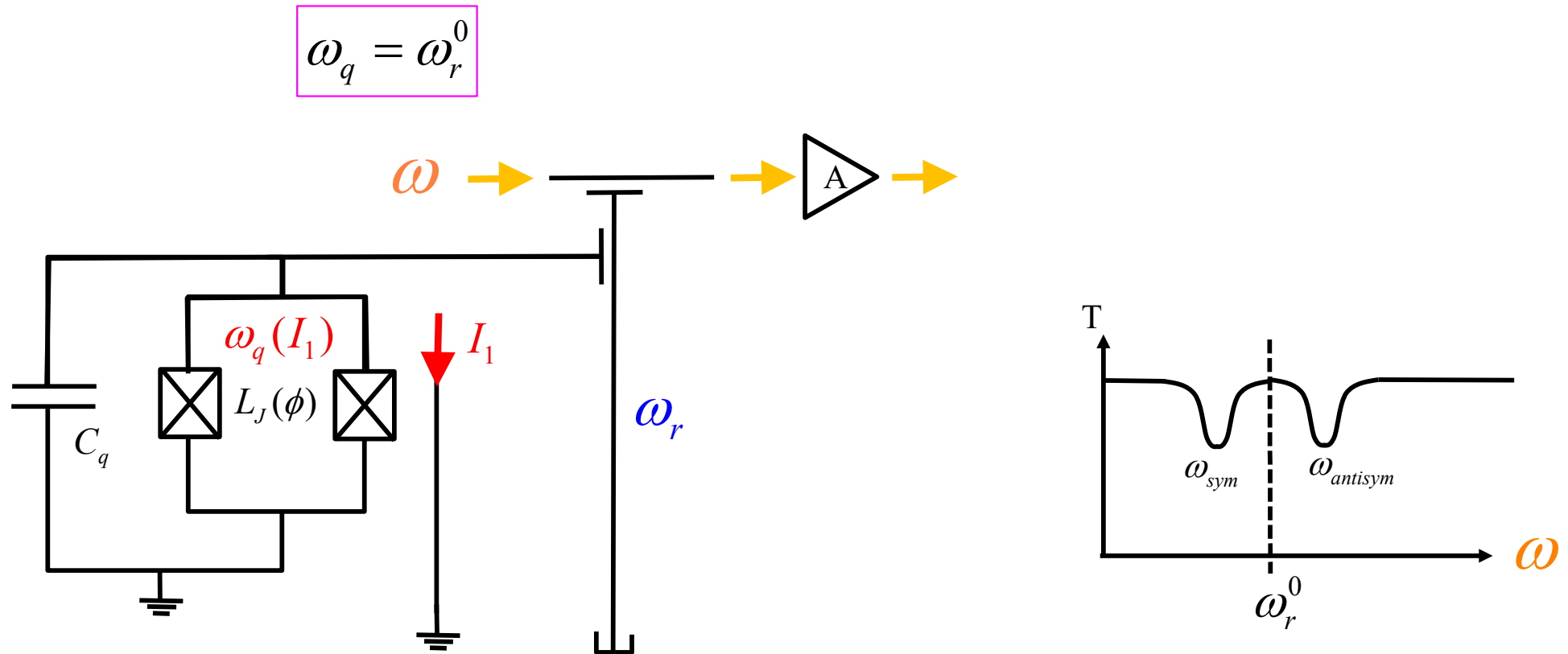
$$P_g \equiv |\langle g | \psi \rangle|^2 = \frac{1 + \langle \sigma_z \rangle}{2}$$

$$P_e \equiv |\langle e | \psi \rangle|^2 = \frac{1 - \langle \sigma_z \rangle}{2}$$

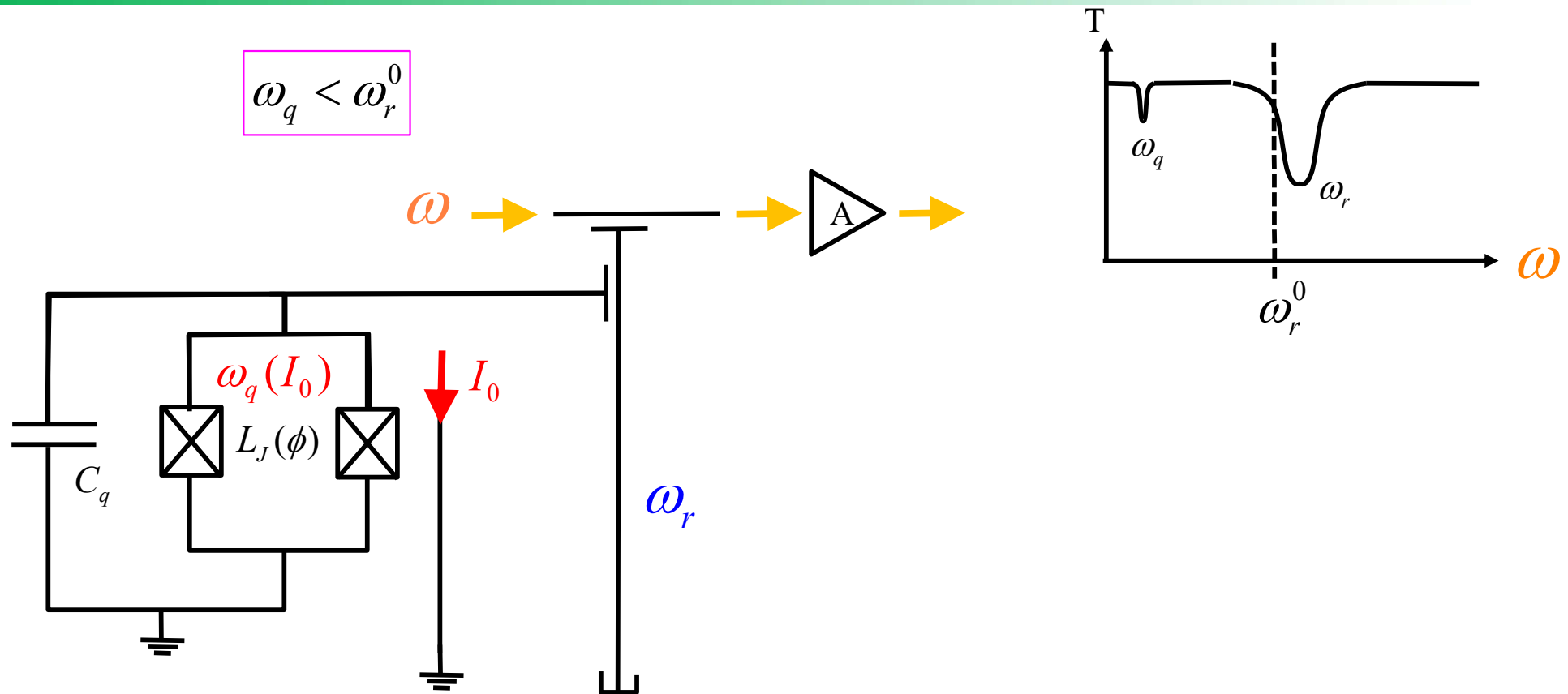
Transmon et résonateur découplés

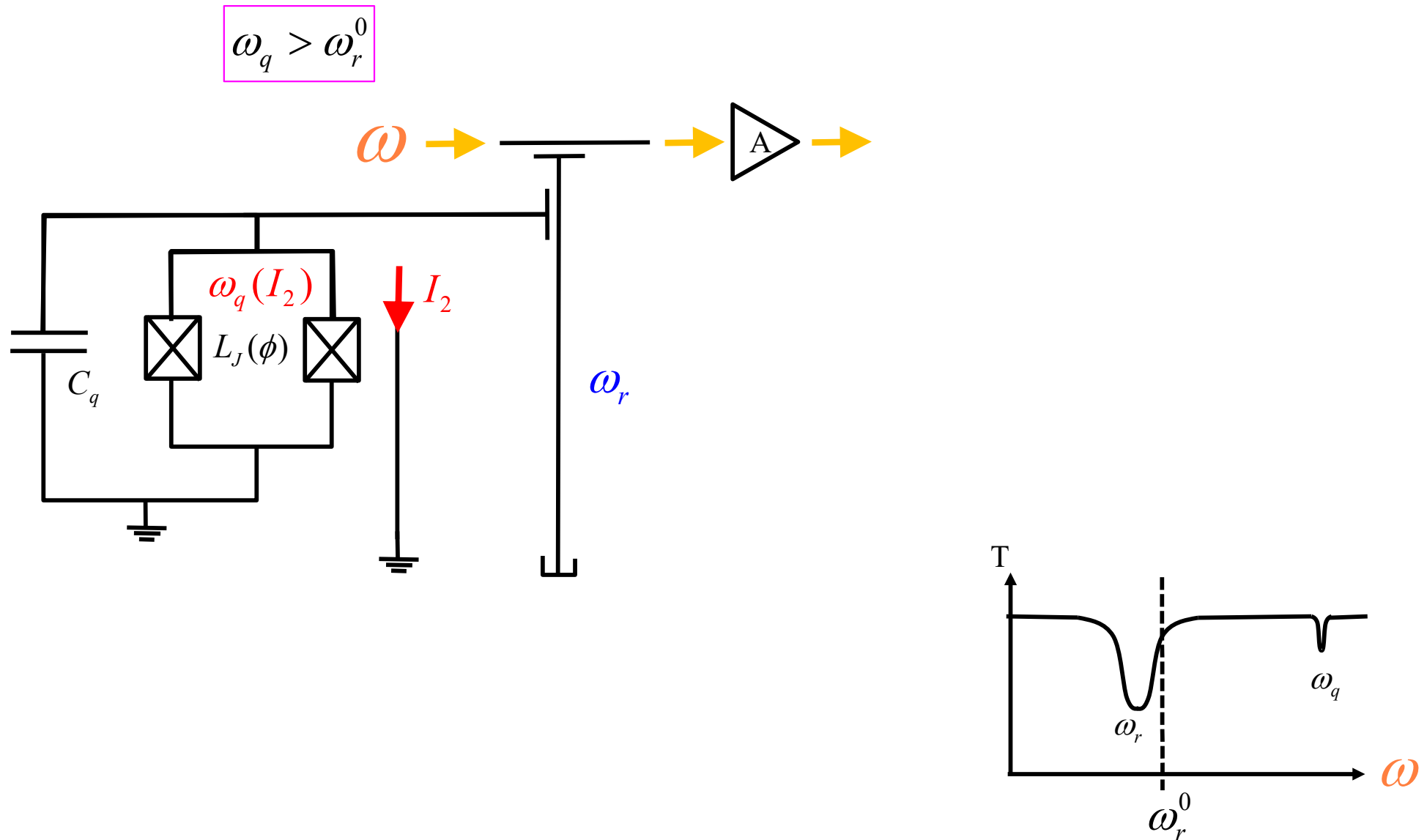


Transmon et résonateur couplés



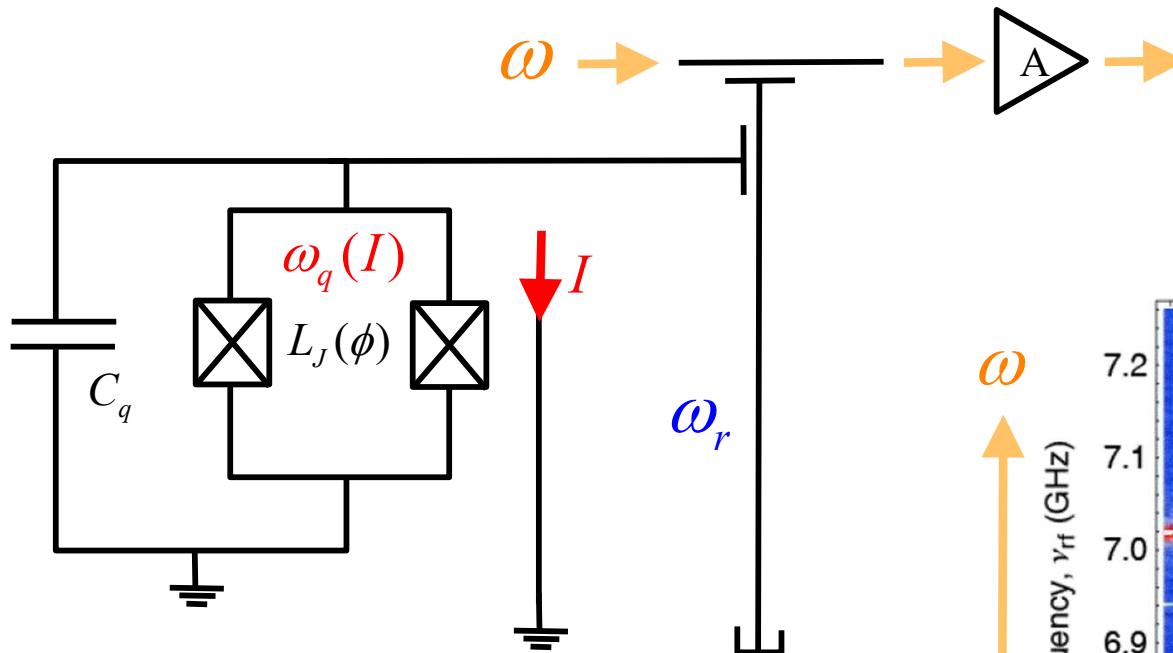
Transmon et résonateur couplés



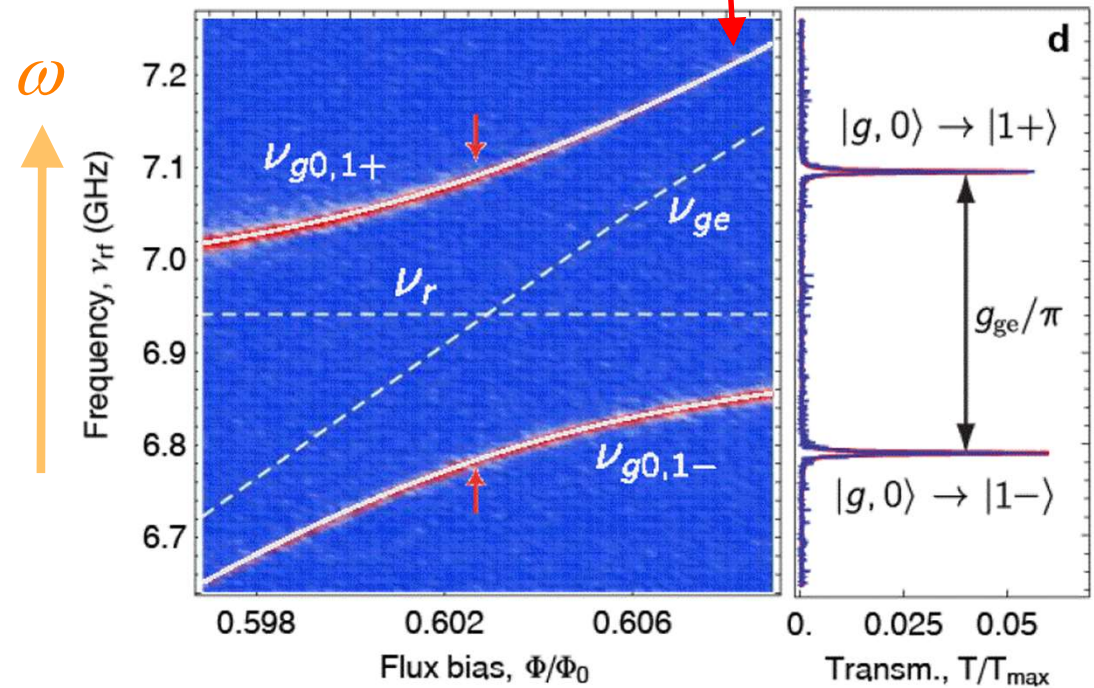


Transmon et résonateur couplés: Mesures en résonnance

J. Fink et al., *Nature (London)* **454**, 315 (2008)



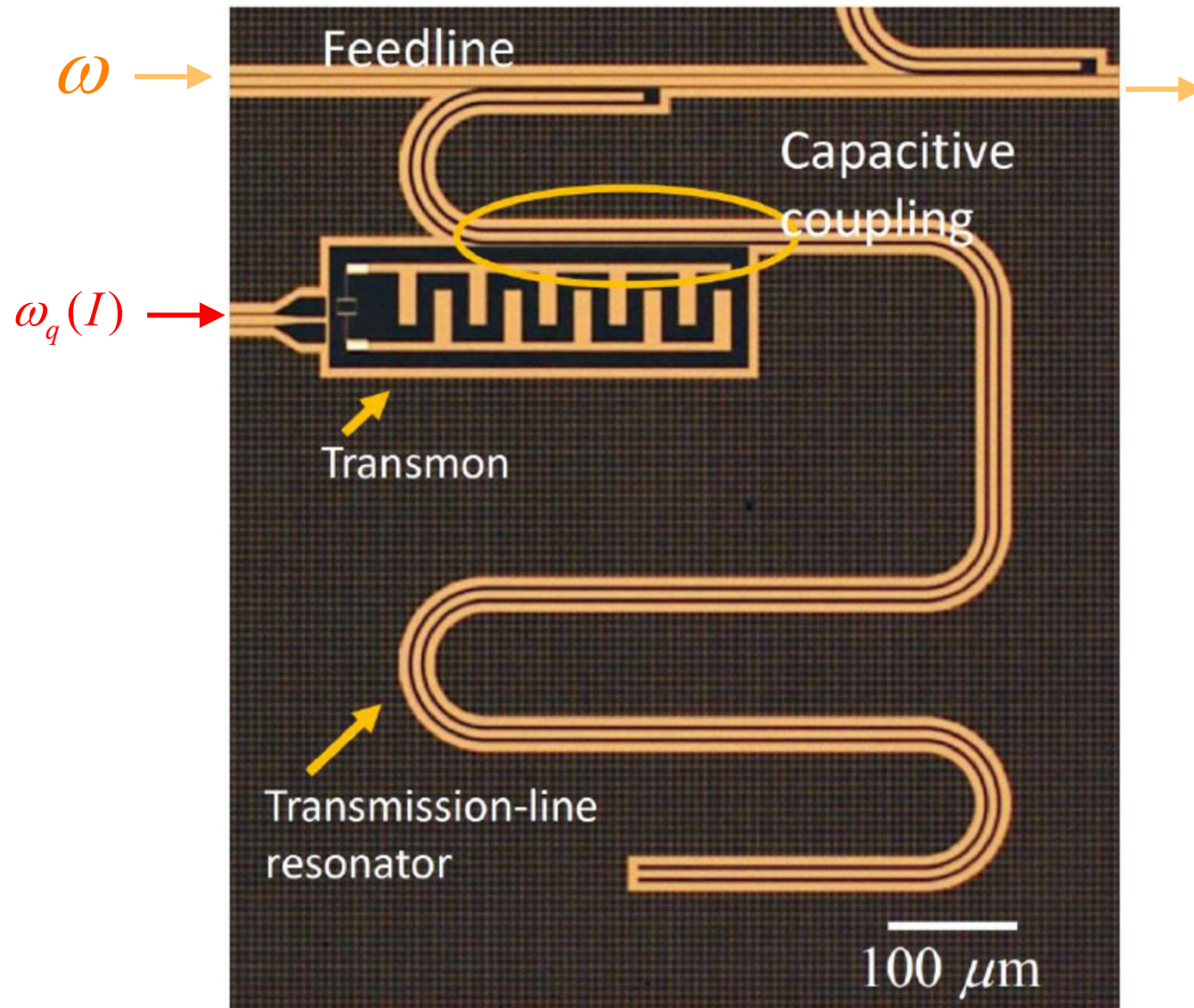
Très faible signal !!



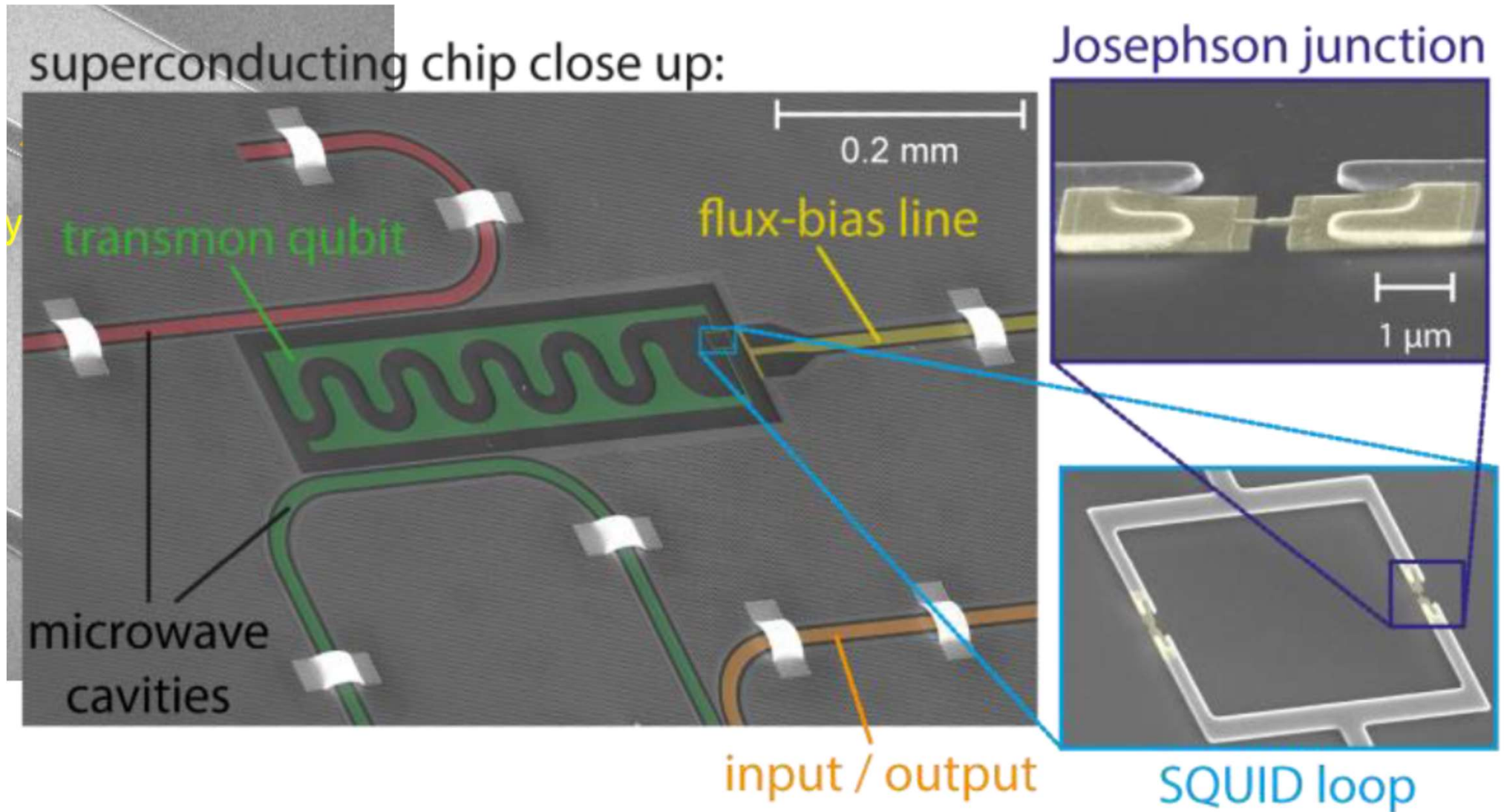
Chaque point de la figure
correspond à une moyenne
sur env. 10'000 mesures

I

Transmons et résonateur couplés: exemples



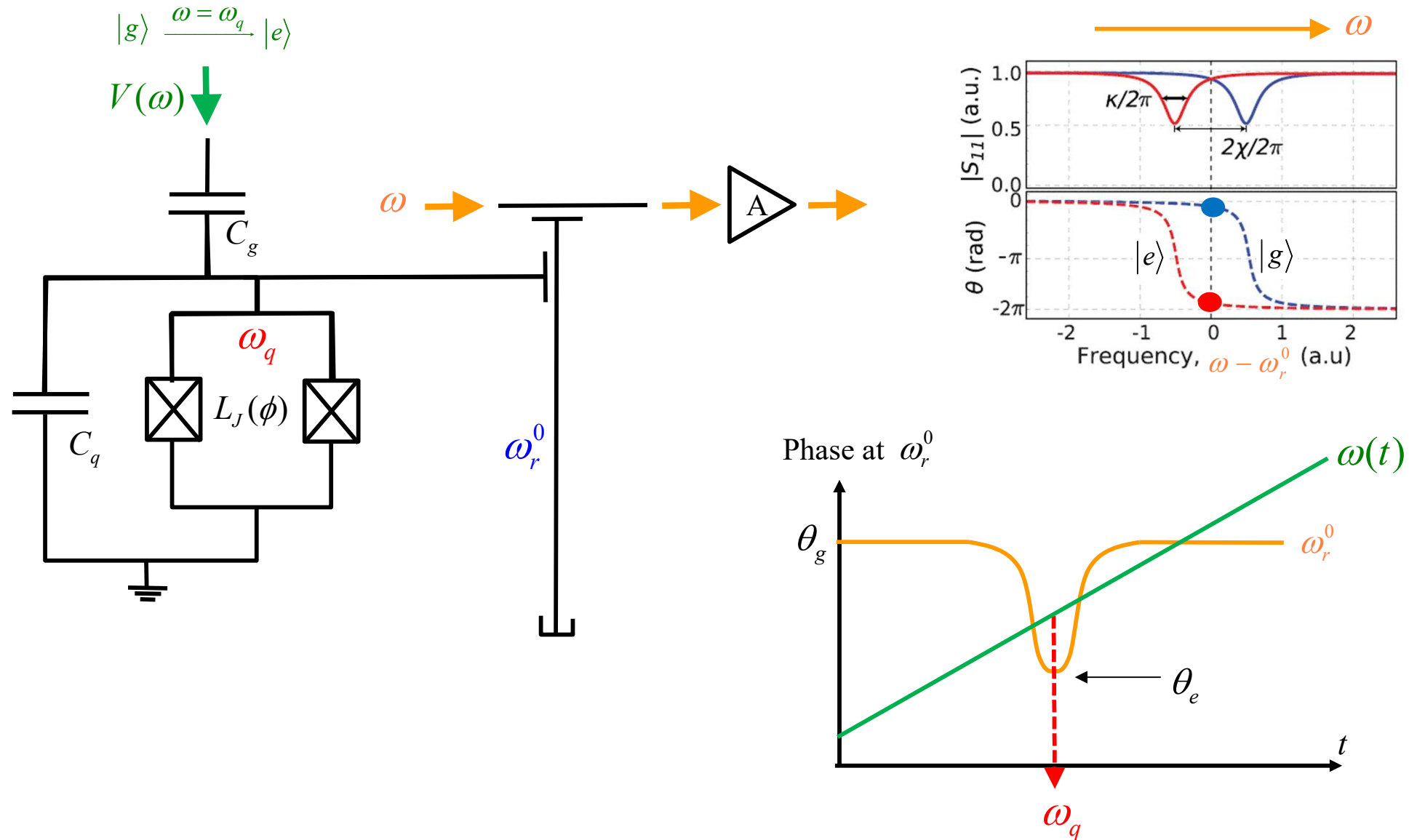
Transmon et résonateur couplés: exemples



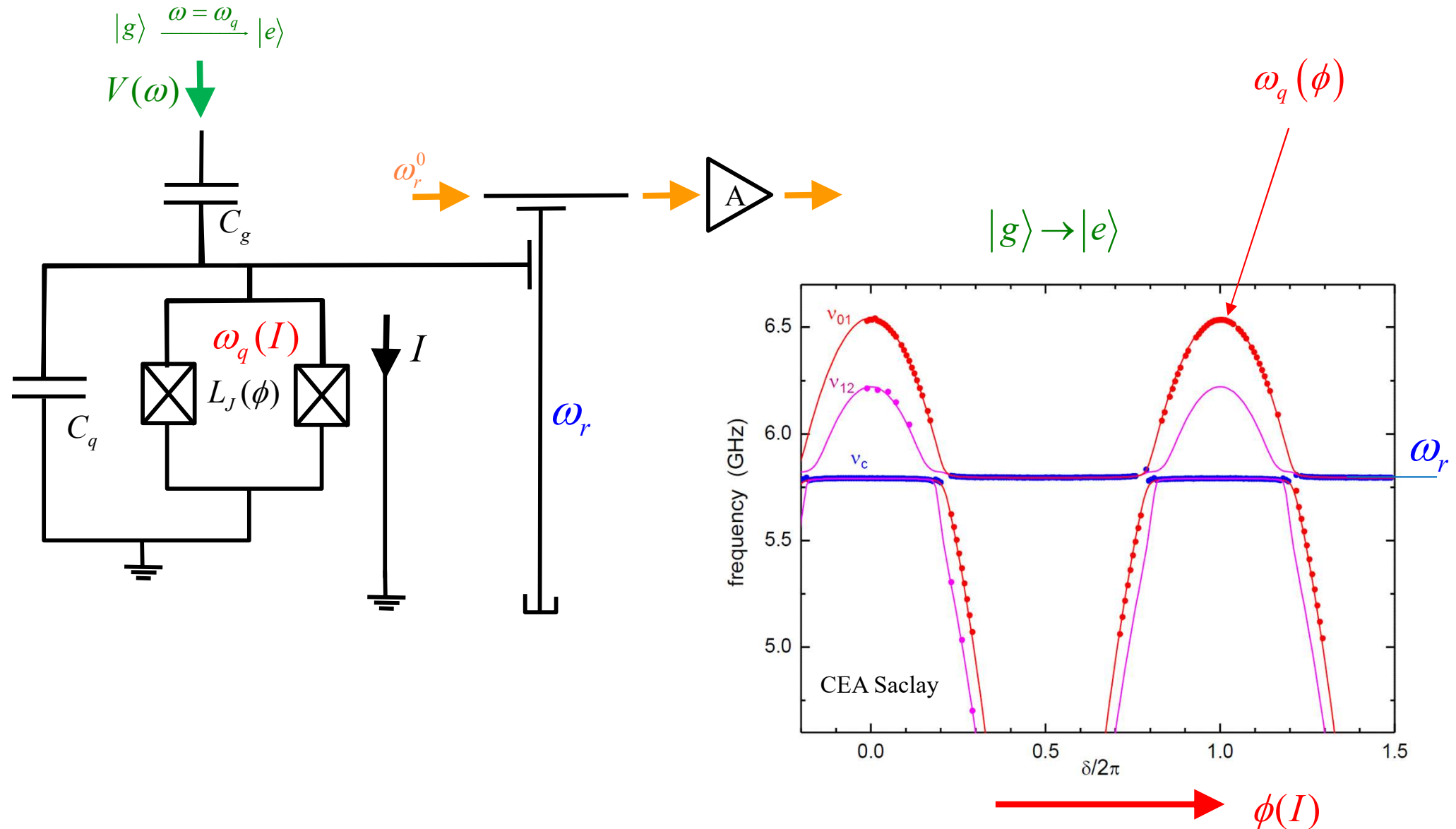
<https://blog.qutech.nl/2017/08/13/how-to-make-artificial-atoms-out-of-electrical-circuits-part-ii-circuit-quantum-electrodynamics-and-the-transmon/>

**Qubit supraconducteur:
Régime dispersif et
Mesures en quantum non-demolition**

Transmon et résonateur en régime dispersif déterminer la fréquence de résonance du qubit

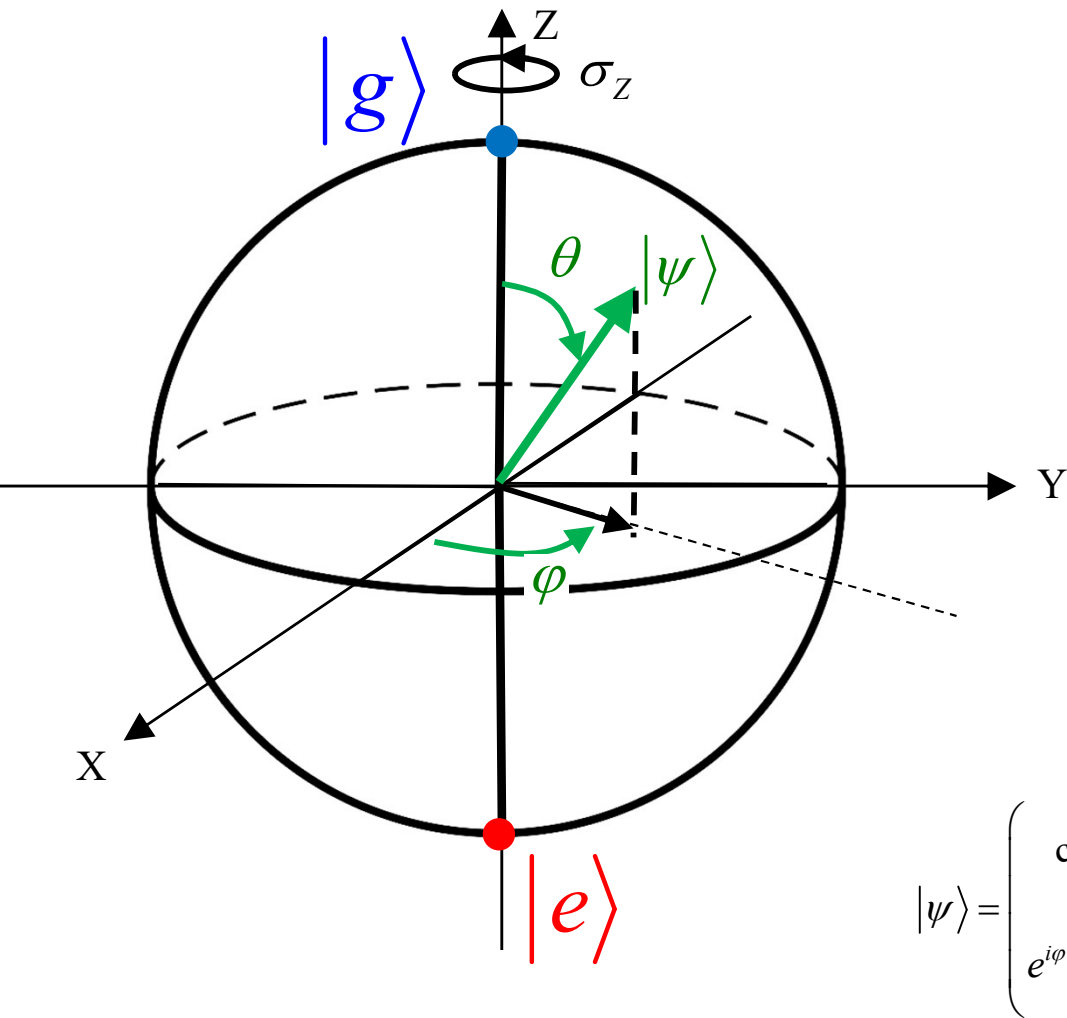


Transmon et résonateur en régime dispersif déterminer la fréquence de résonance du qubit

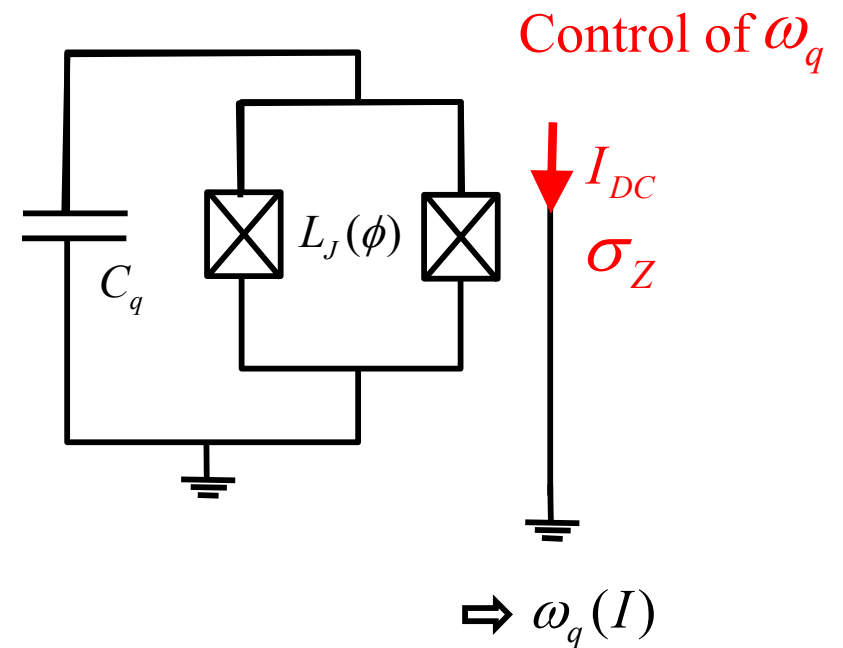


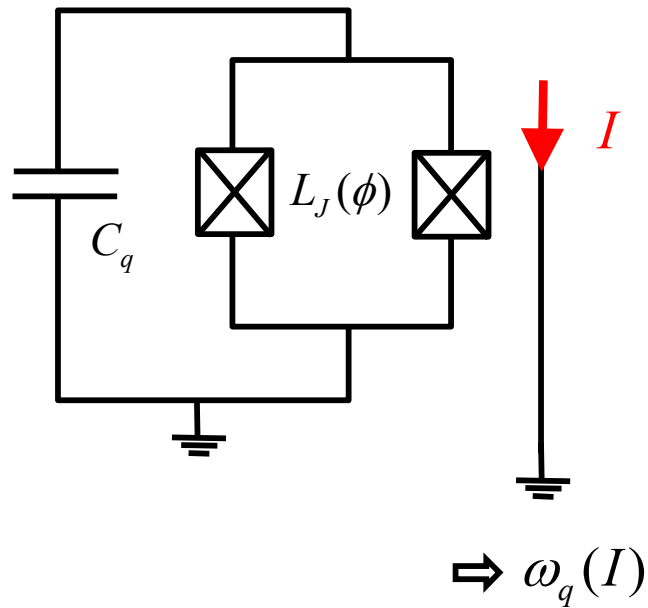
Qubit supraconducteur:

Rotation σ_Z

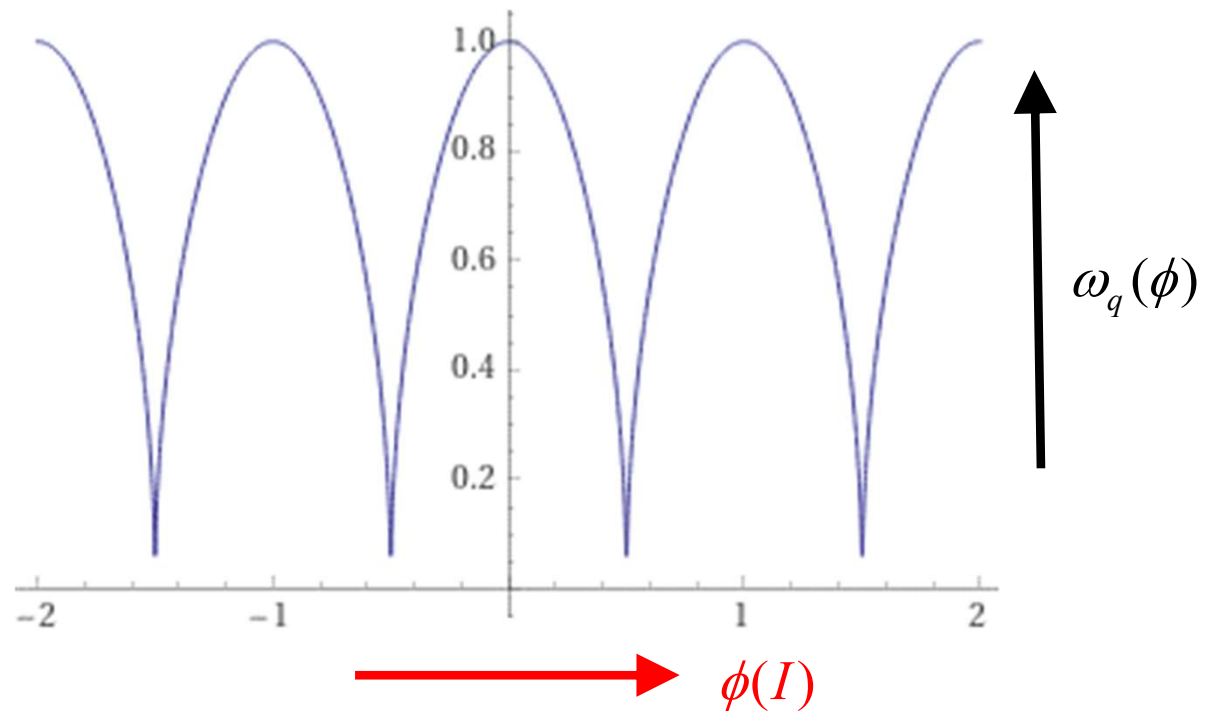


$$\omega_q(\phi) \equiv \frac{1}{\sqrt{L_J(\phi)C_q}}$$





$$\omega_q(\phi) \equiv \frac{1}{\sqrt{L_J(\phi)C_q}} \approx \sqrt{\left| \cos\left(\frac{1}{\pi} \cdot \frac{\phi}{\phi_0}\right) \right|}$$



Qubit supraconducteur:

Rotation σ_X et σ_Y

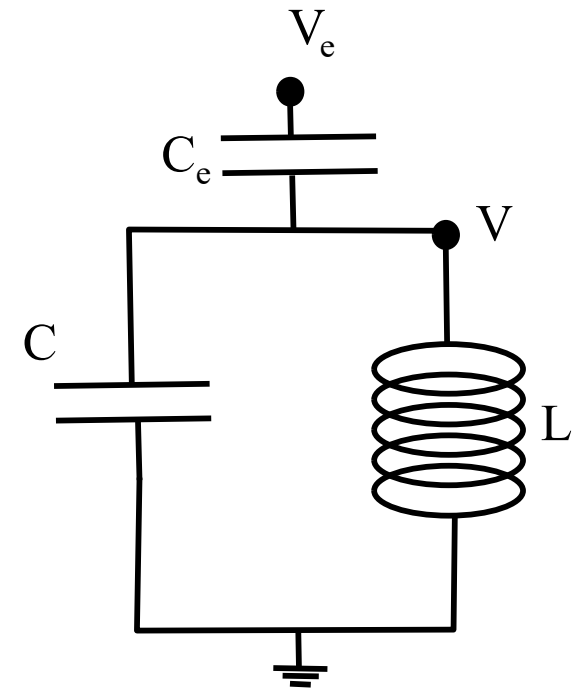
Rappel: Exercice 9.2: Hamiltonien d'excitation

Oscillateur Harmonique LC

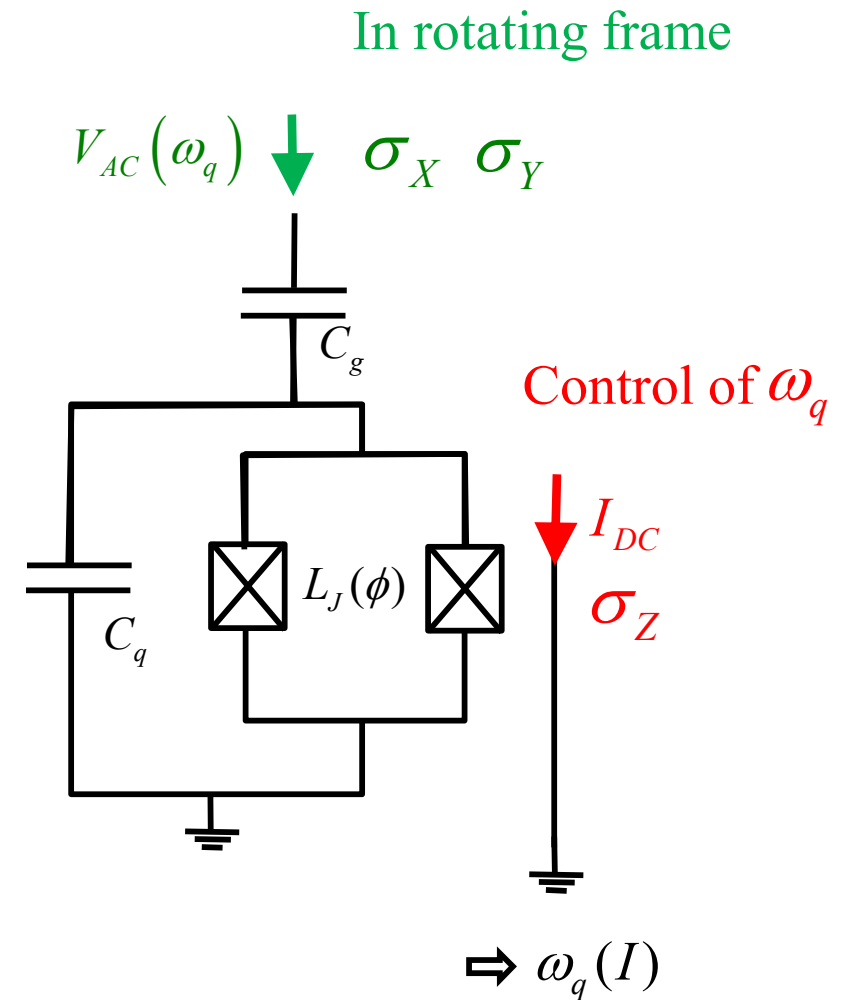
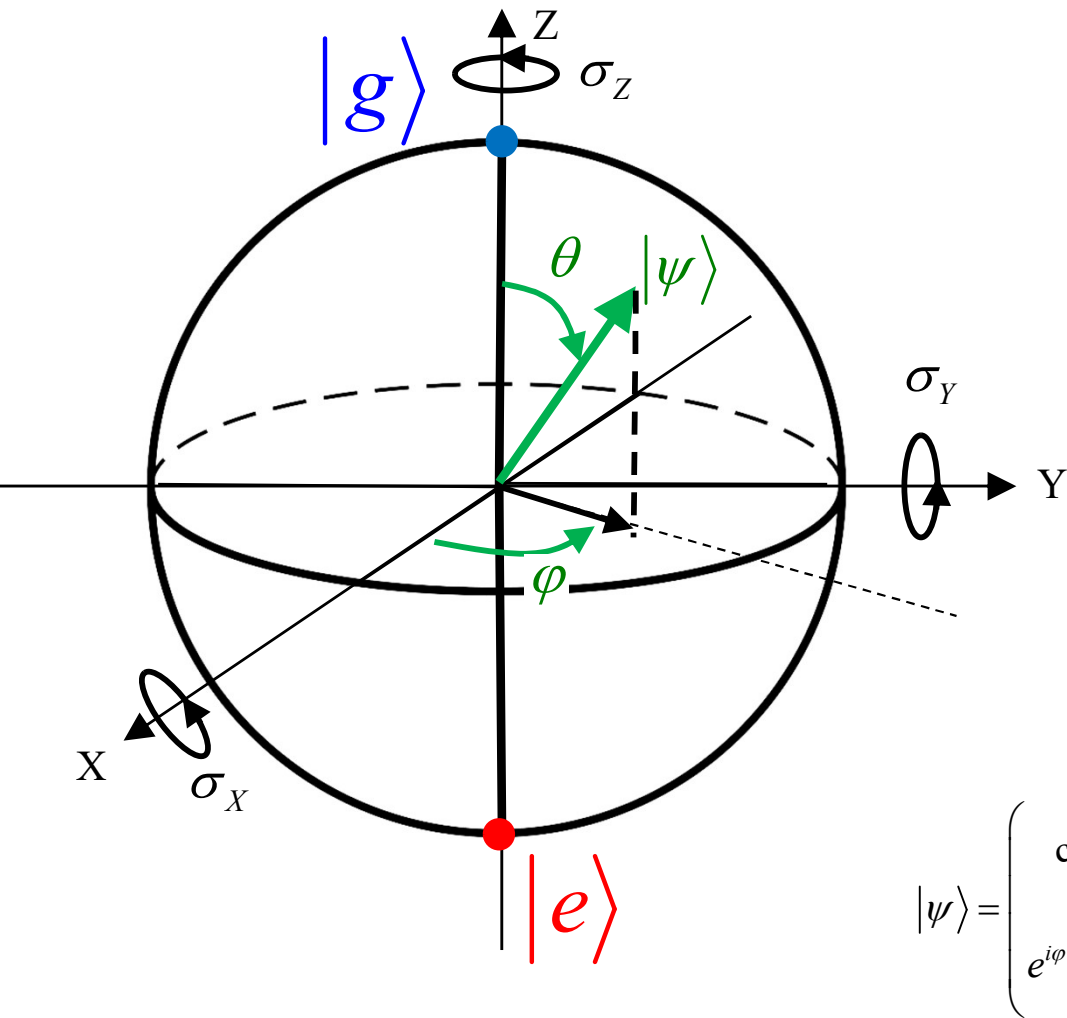
$$H_e \approx -C_e \cdot V_e \cdot V = -C_e \cdot V_e \cdot \frac{Q}{(C + C_e)}$$

$$H_e \approx \frac{C_e}{C + C_e} \cdot V_e \cdot \left(\frac{\hbar^2 \cdot (C + C_e)}{4 \cdot L} \right)^{1/4} \cdot i \cdot (a_+ - a_-)$$

$$H_e = g \cdot V_e \cdot \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} = g \cdot V_e \cdot \sigma_Y$$

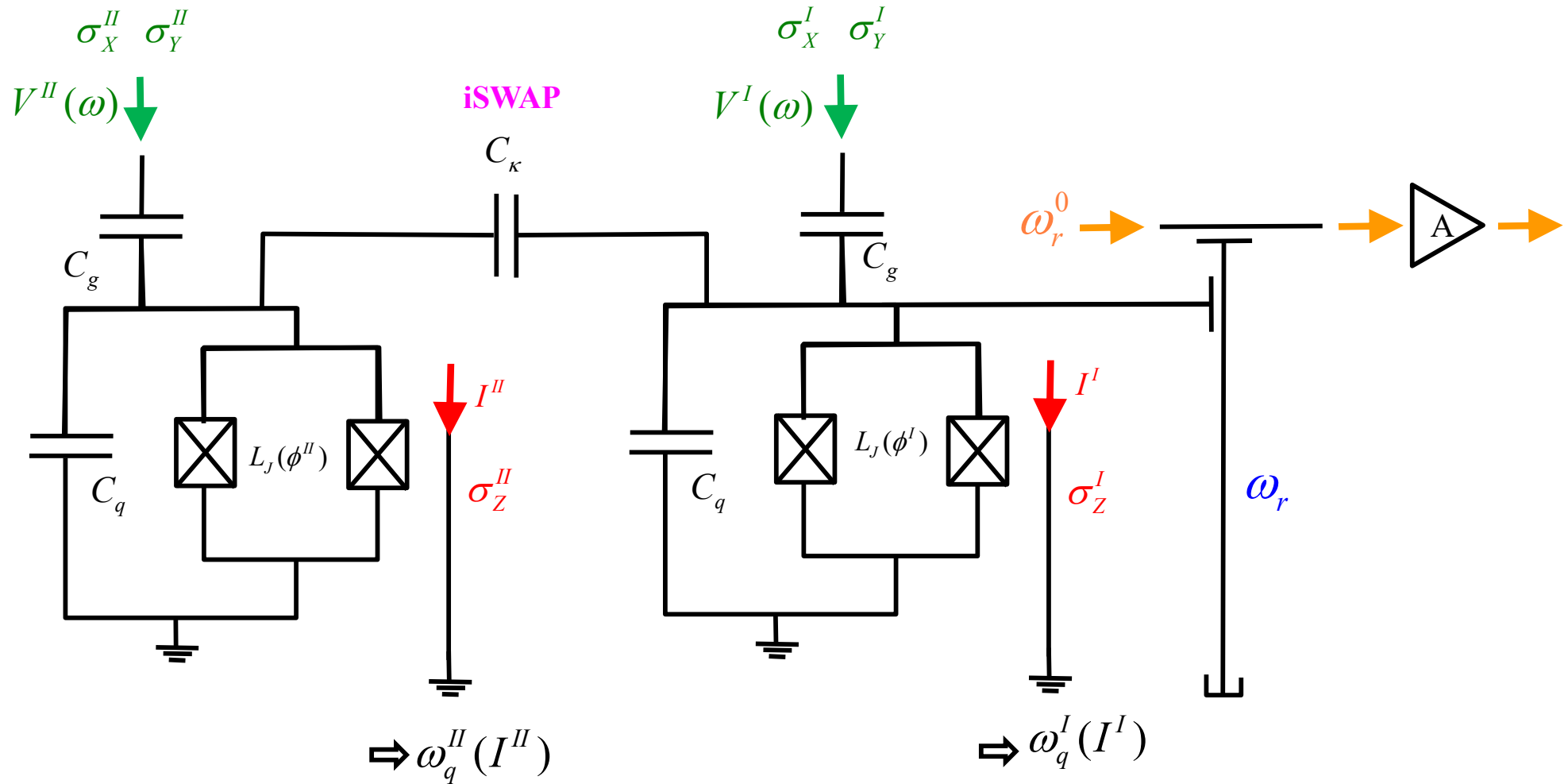


Contrôle par couplage capacitif AC dans le référentiel tournant

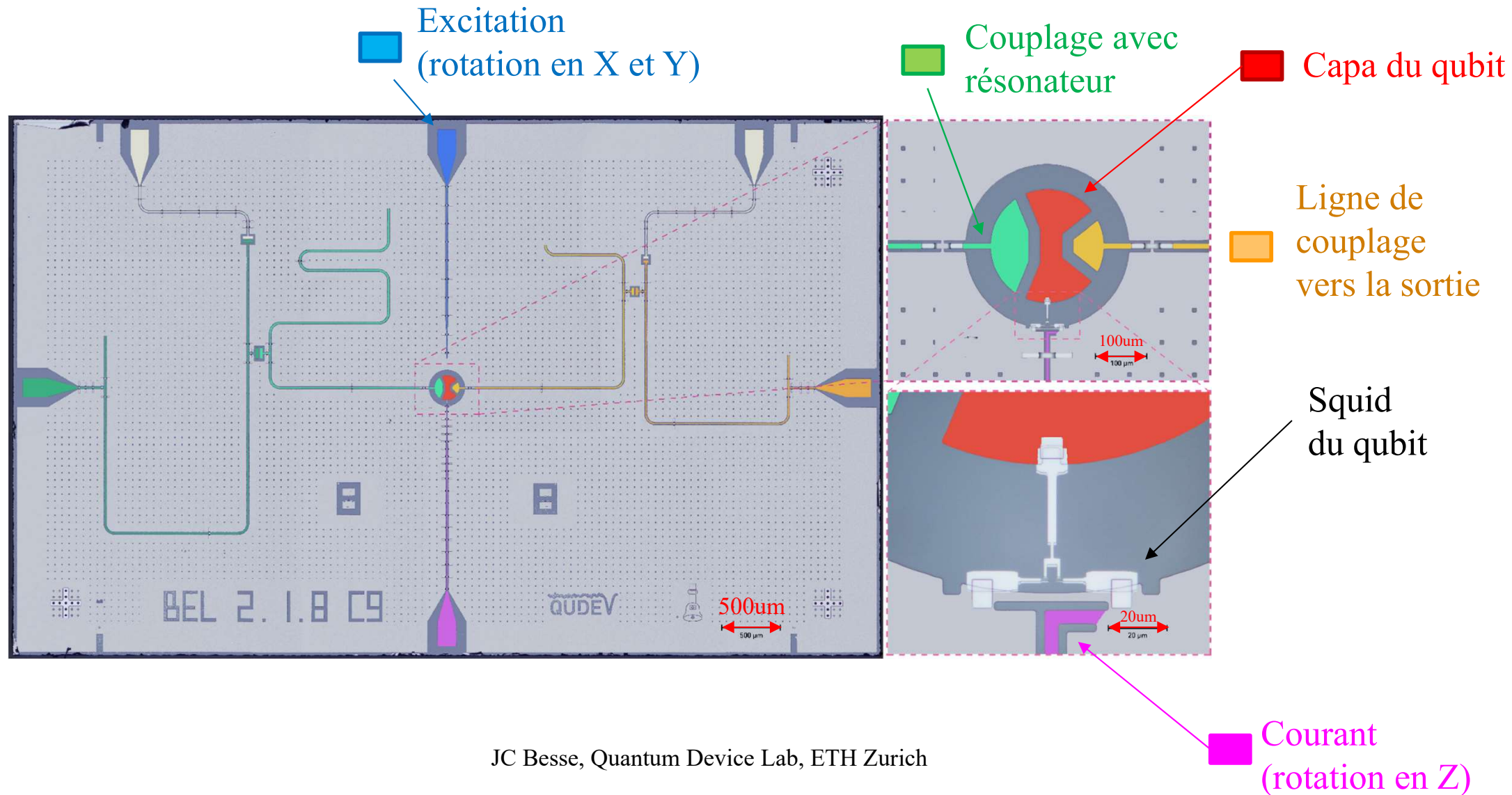


**Qubit supraconducteur:
Paire de qubits couplés
(iSWAP)**

Paire de Qubits couplés

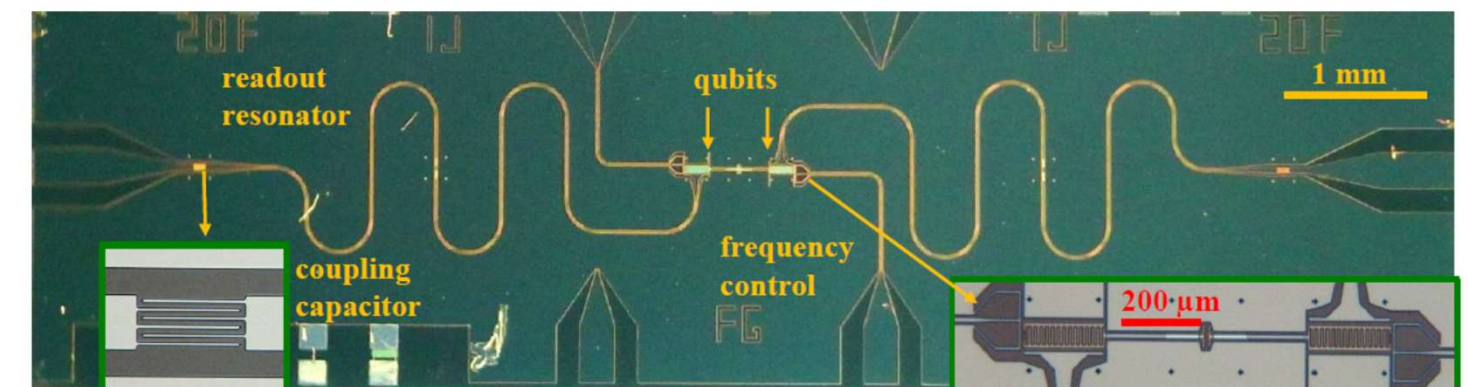
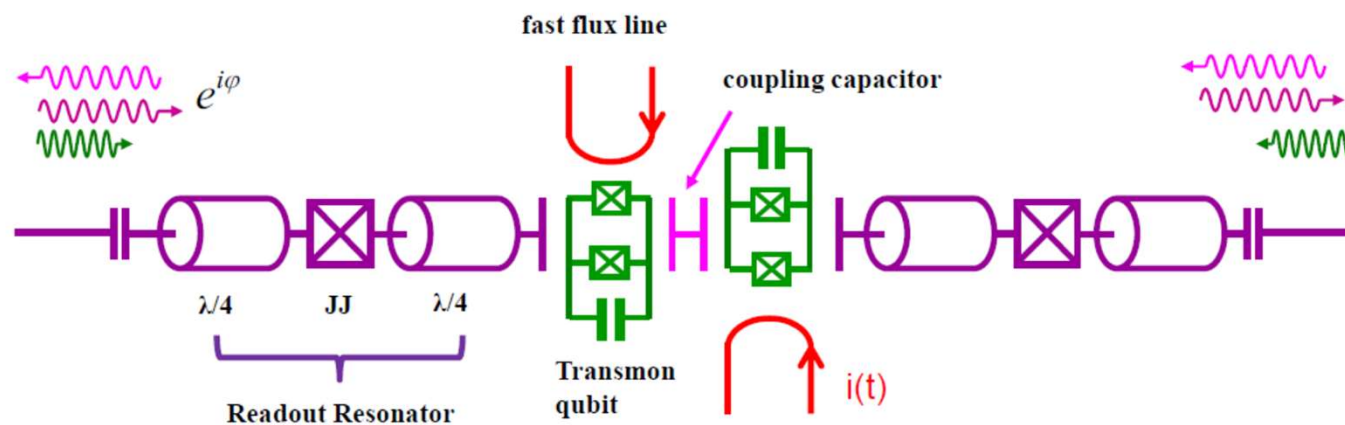


Devices et setup de mesure: exemples

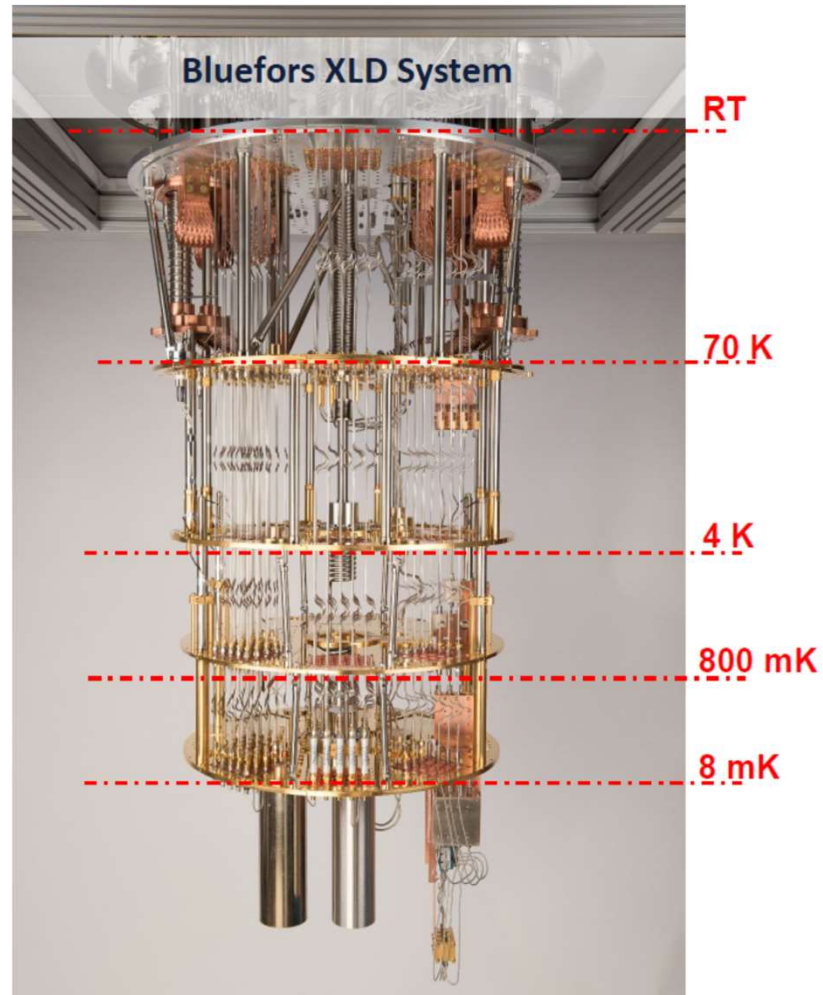


Example : capacitively coupled transmons with individual readout

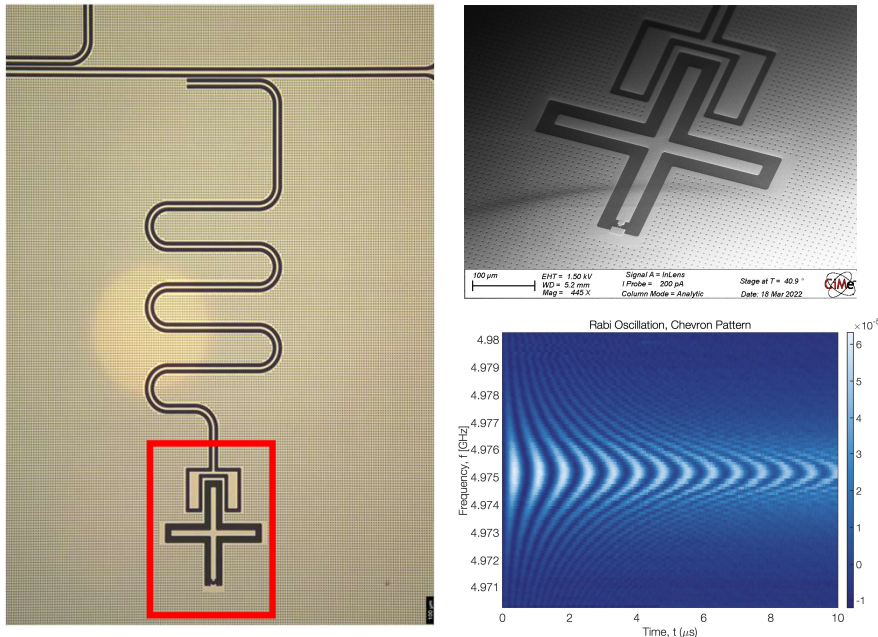
(Saclay, 2011)



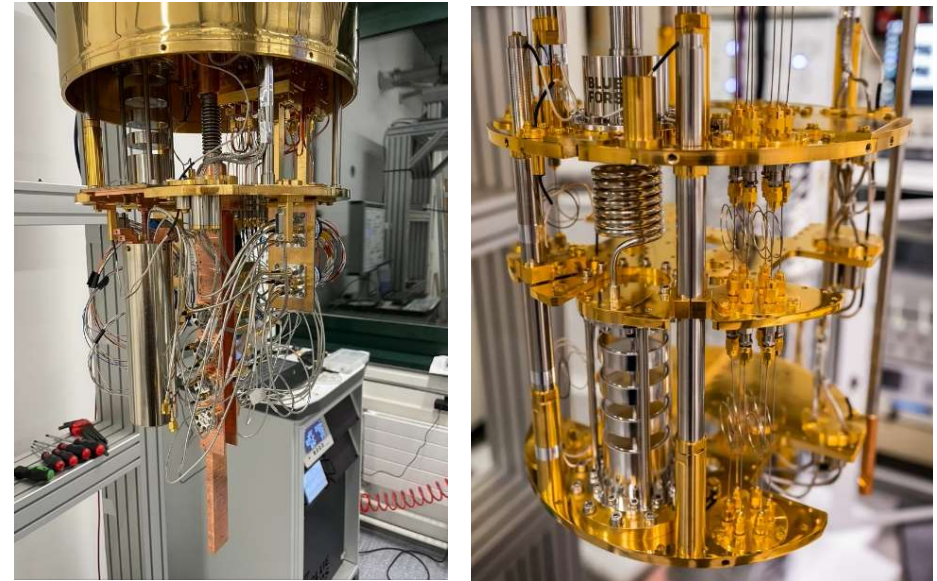
Mesures en cryogénie



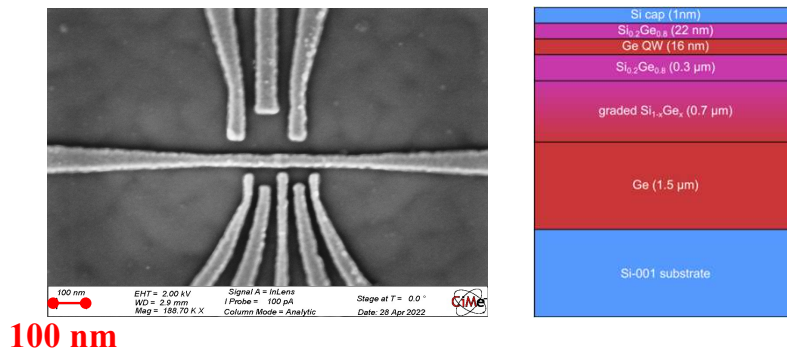
Aluminium Transmon Qubits



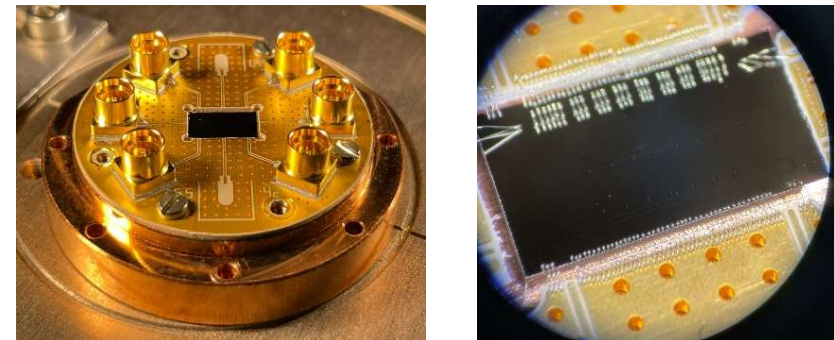
10 mK Dilution Refrigerator in HQC



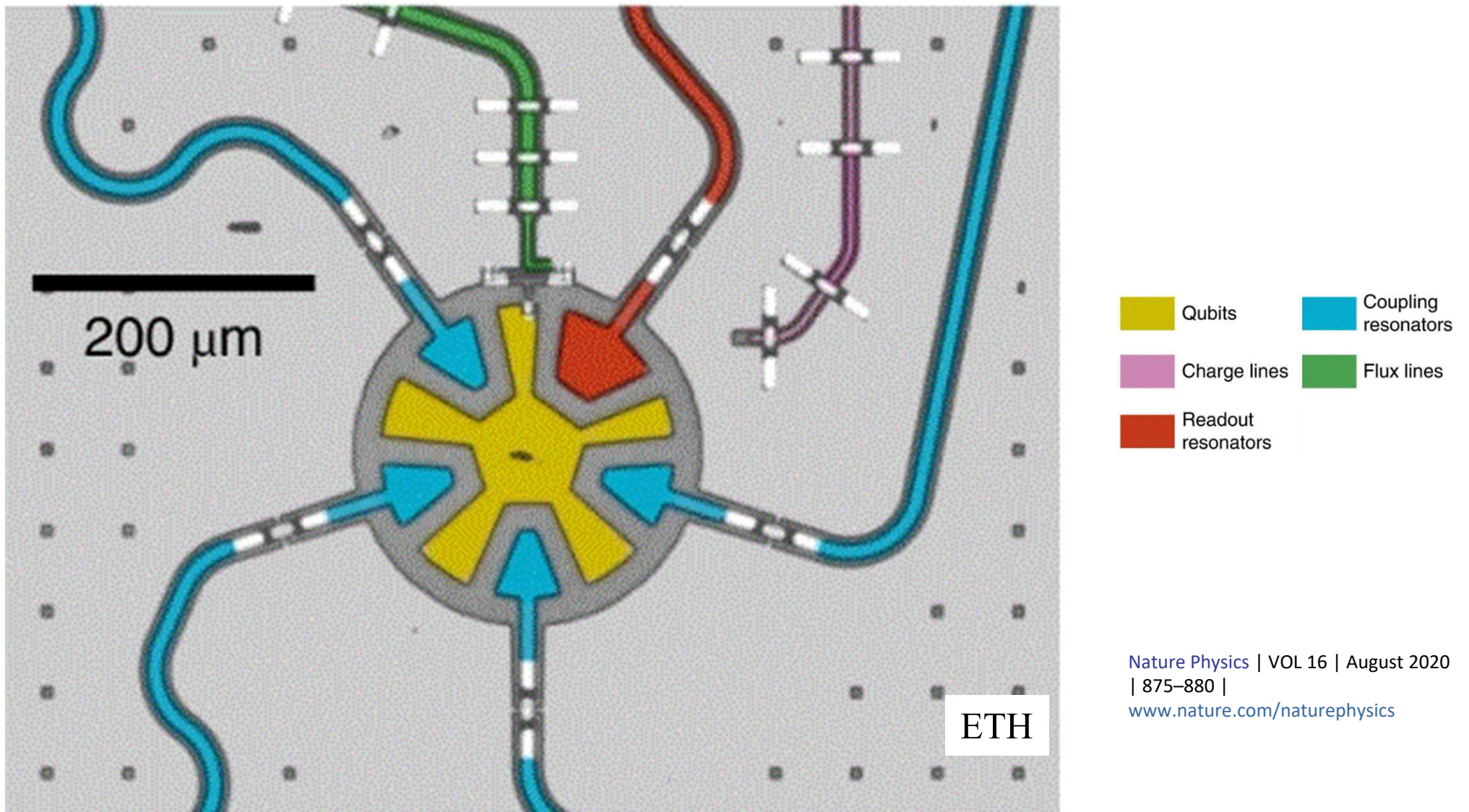
Quantum Dots in Germanium Heterostructures



5-10 GHz Printed Circuit Board hosting the device

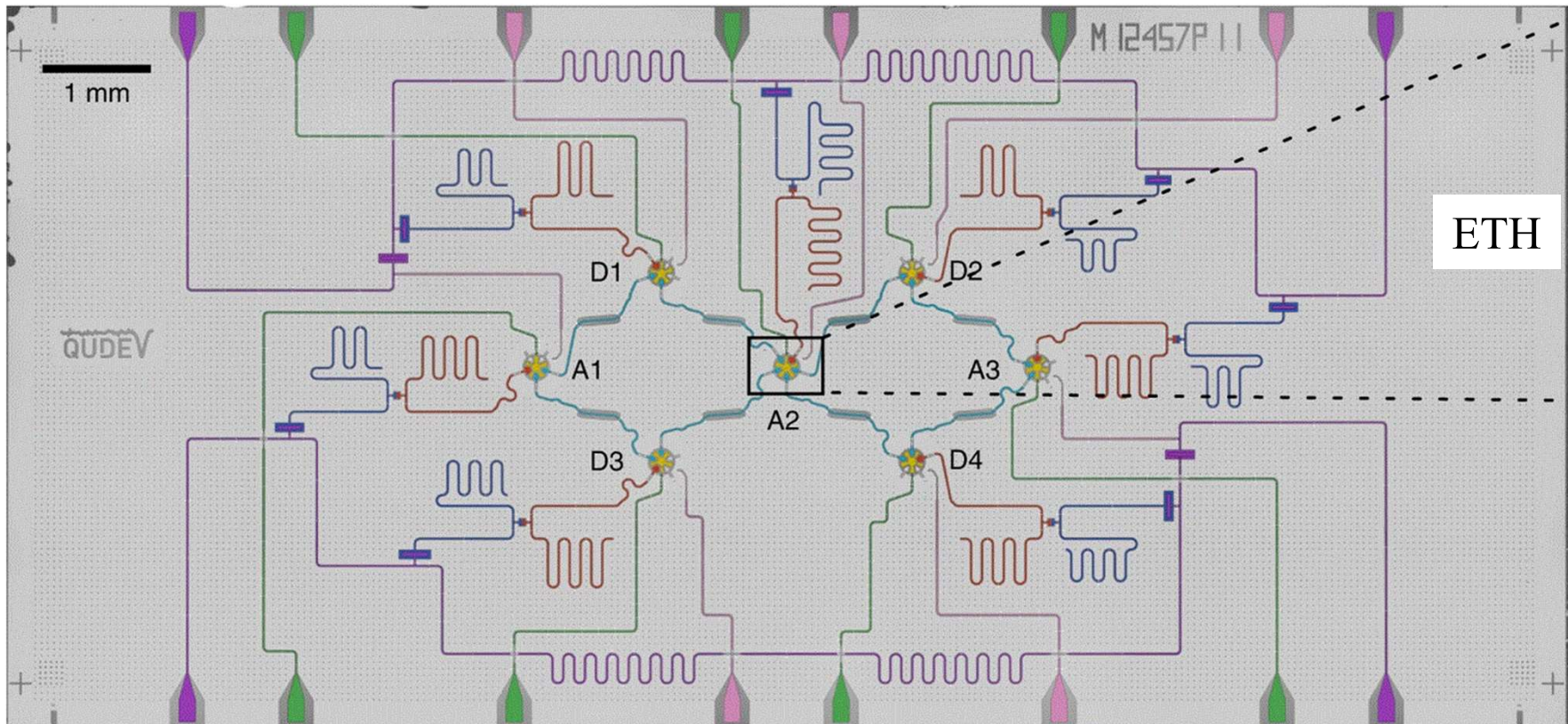


Qubit et lignes de couplage



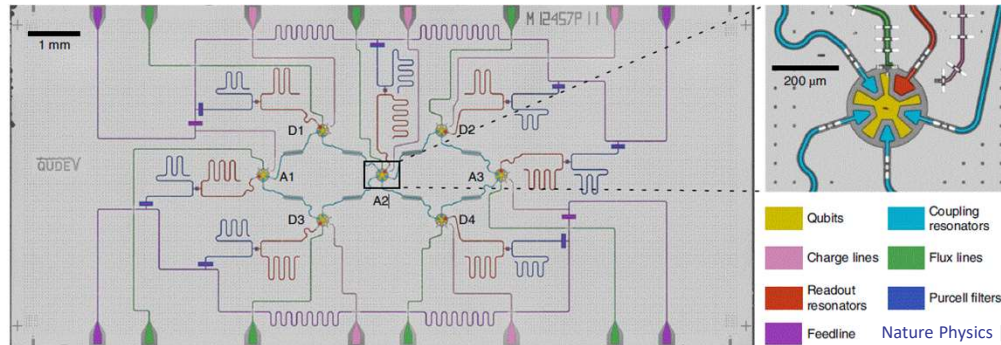
Nature Physics | VOL 16 | August 2020
| 875–880 |
www.nature.com/naturephysics

Puce avec 7 qubits



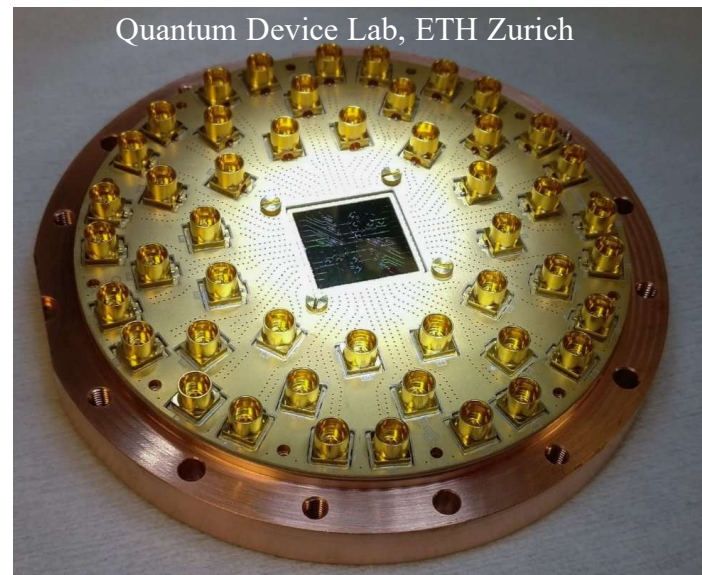
Nature Physics | VOL 16 | August 2020
| 875–880 | www.nature.com/naturephysics

Ordinateur Quantique: ETH



5-10 GHz
10 mK

Nature Physics | VOL 16 | August 2020
| 875–880 | www.nature.com/naturephysics

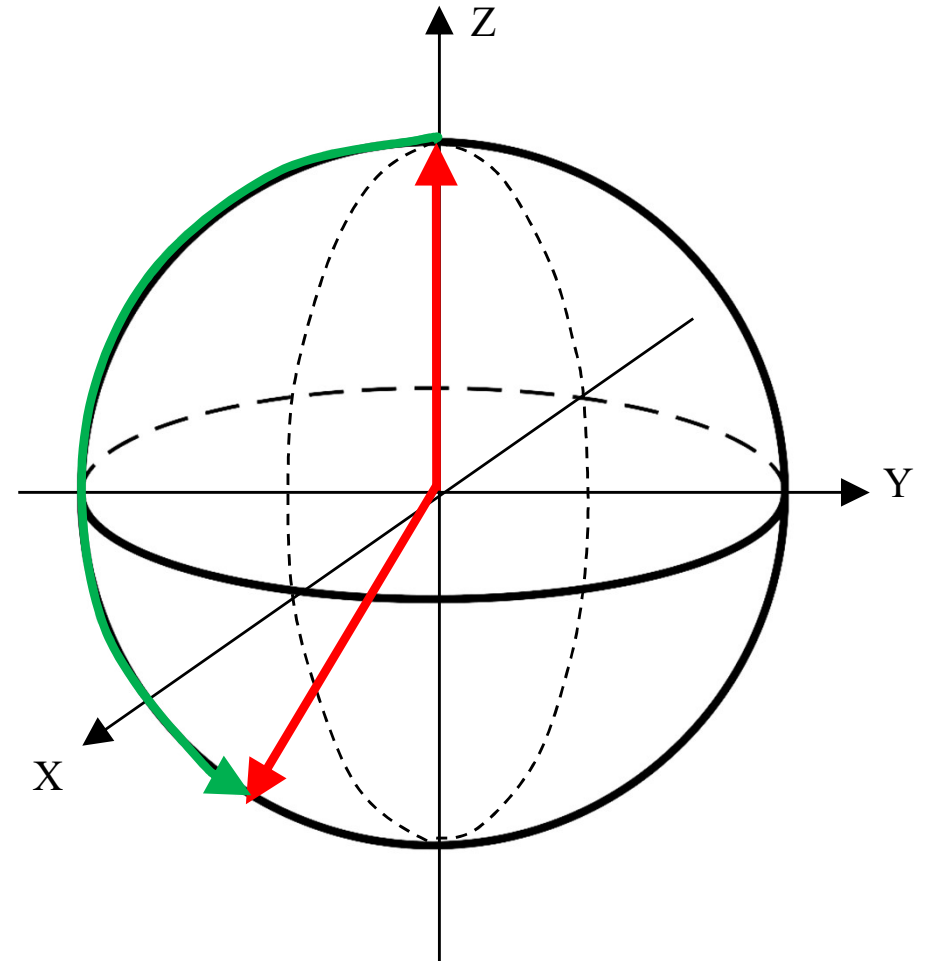
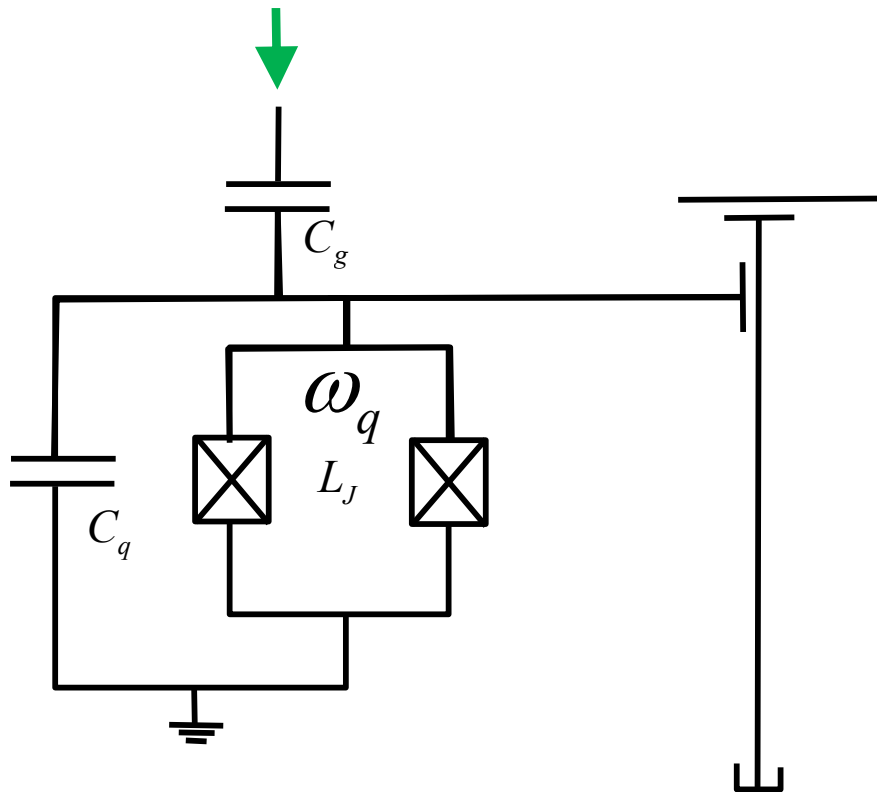


Mesures de Qubits:

- **Fréquence de Rabi**
- **Relaxation, mesures de T_1**
- **Décohérence**

1) Fréquence de Rabi: Excitation

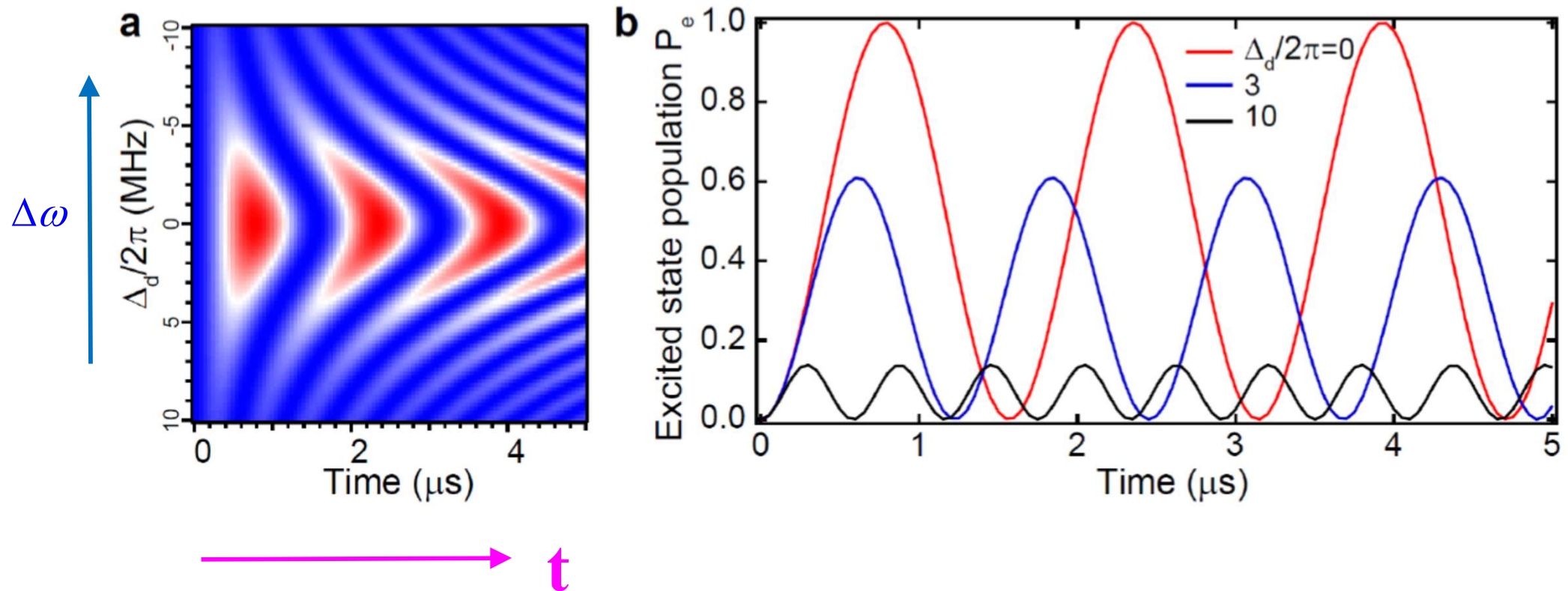
$$V(\omega) = T \cdot \cos(\omega \cdot t)$$



1) Fréquence de Rabi: Résultats

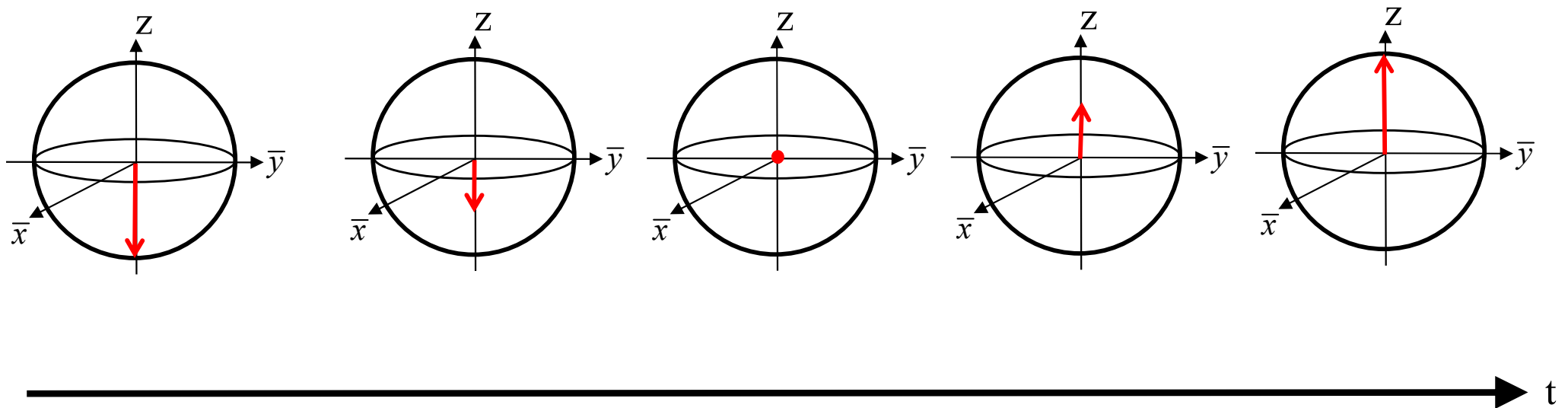
$$\Delta\omega \equiv \omega - \omega_q$$

Chaque point de la figure
correspond à une moyenne
sur env. 10'000 mesures

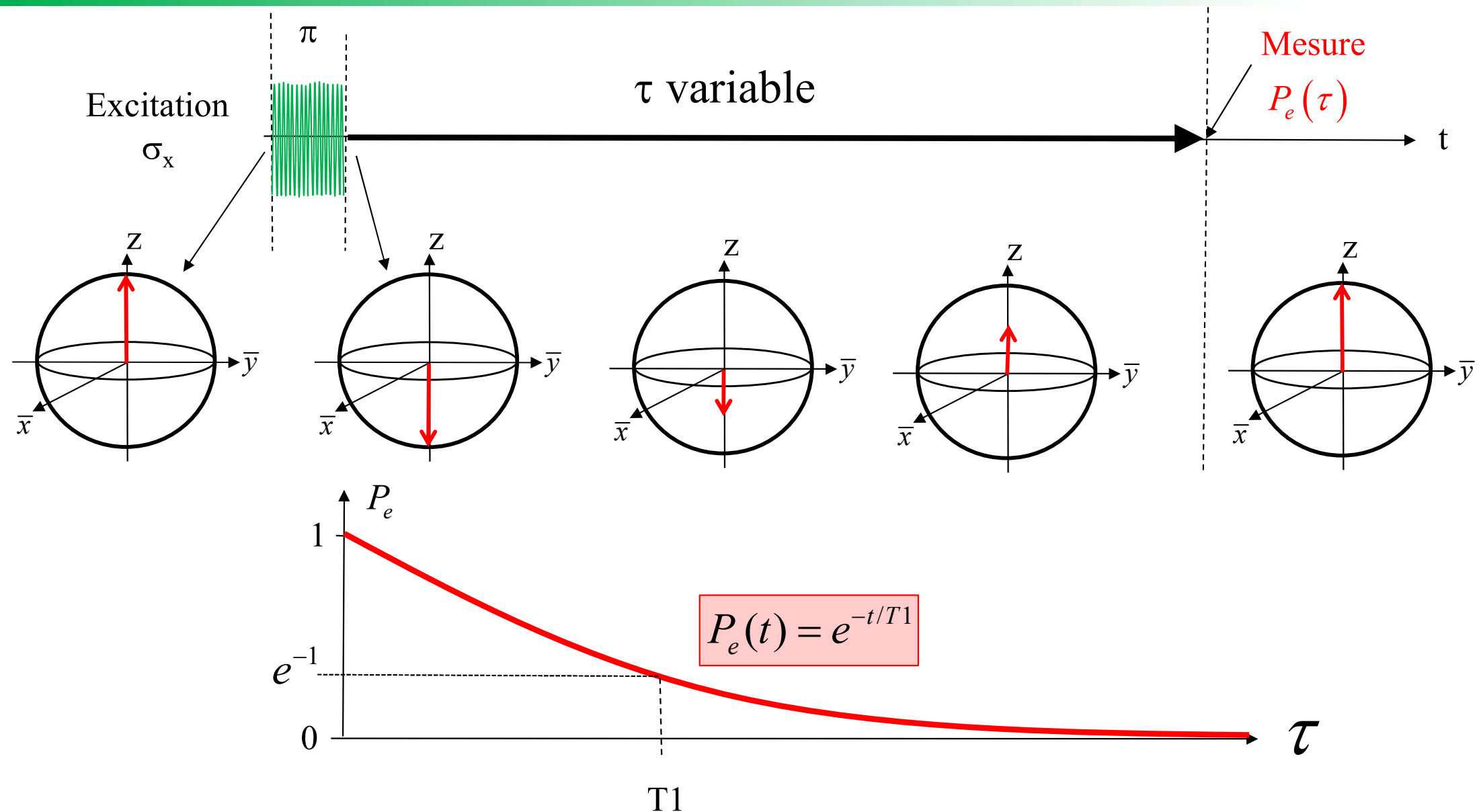


2) Relaxation

Relaxation: Temps T1

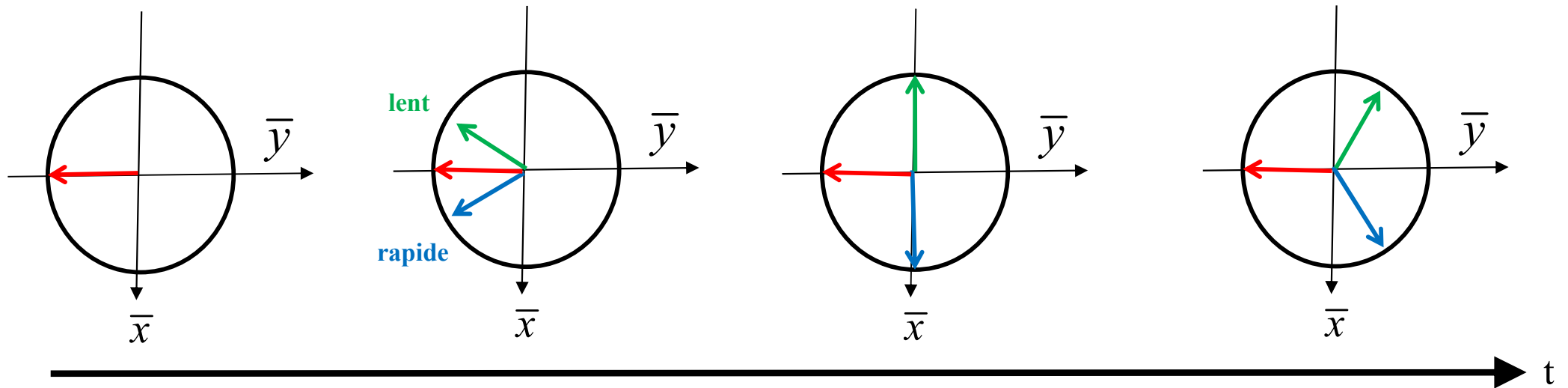


2) Mesure du temps de relaxation T1

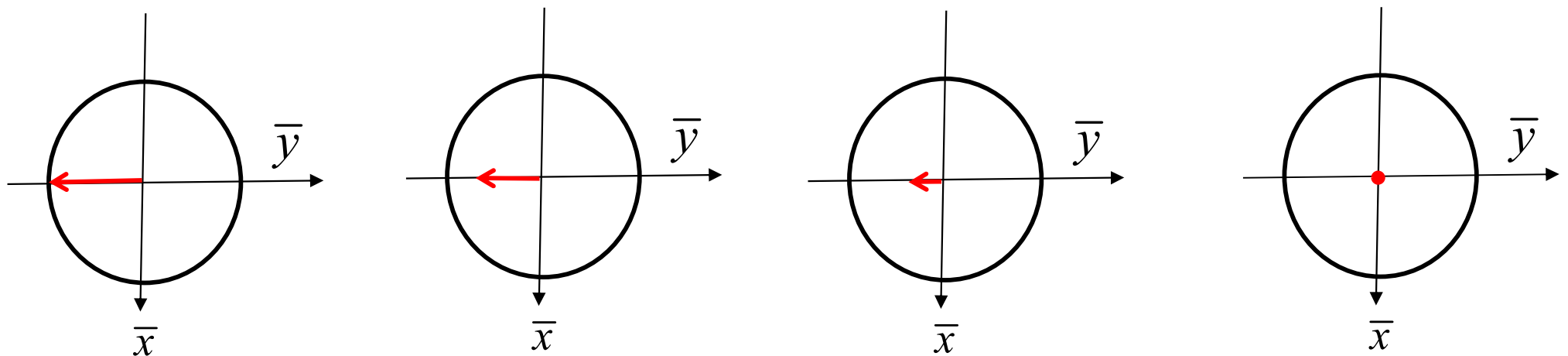


3) Décohérence dans le plan X,Y

Décohérence: Temps T_2^* (T_2)

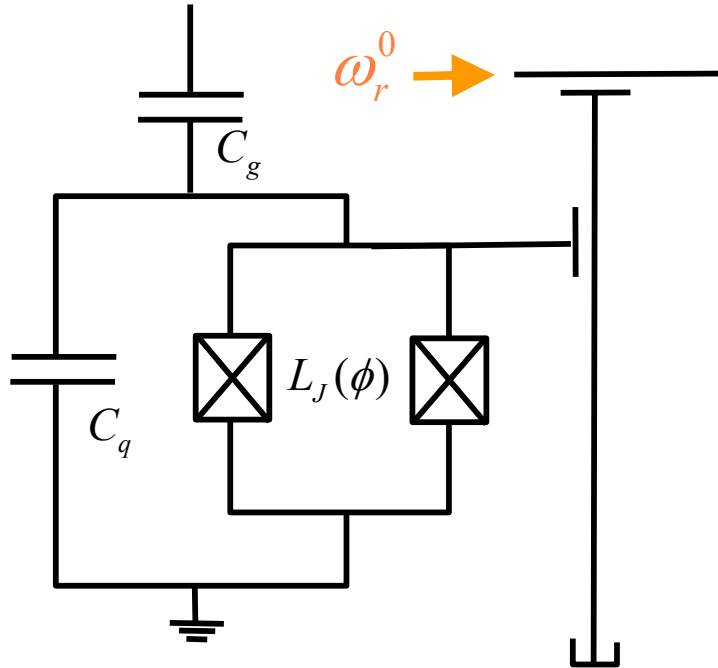


Qubit moyen



Exercices

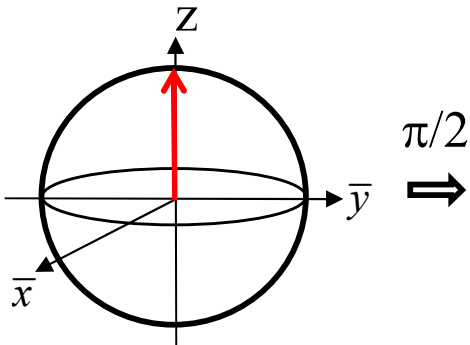
Exercice 13.1: mesure par quantum non-demolition



Le qubit est dans l'état de base,

- Nous appliquons une impulsion en X de $\pi/2$
- Nous faisons directement (en négligeant la relaxation et la décohérence) une mesure par quantum non-demolition.

Indiquez, sur la sphère de Bloch, l'évolution du qubit.



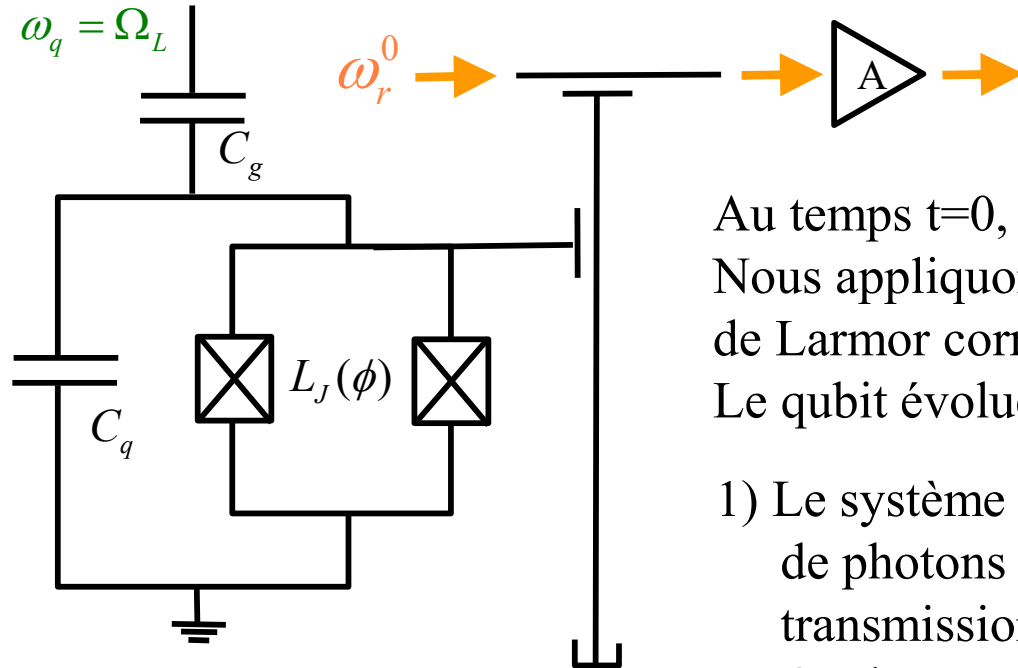
$\pi/2$



Mesure



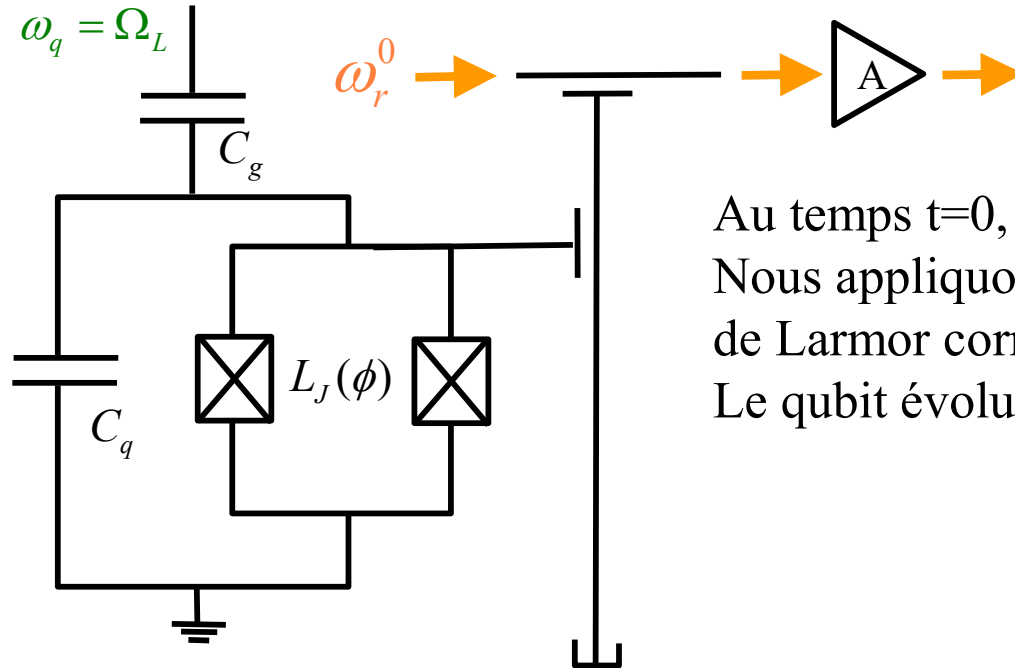
Exercice 13.2: effet Zénon



Au temps $t=0$, le qubit est dans l'état de base,
 Nous appliquons en continu un signal d'excitation à la fréquence
 de Larmor correspondant à la résonance du qubit ($\omega_q = \Omega_L$).
 Le qubit évolue à la fréquence de Rabi Ω_R .

- 1) Le système de mesure par non-démolition (excitation par injection
 de photons dans le résonateur et mesure électronique de la
 transmission) est enclenché à intervalles $\Omega_R.T = \pi$
 Quels sont les signaux détectés ?
 «0» = état de base, «1» = état excité

Exercice 13.2: effet Zénon



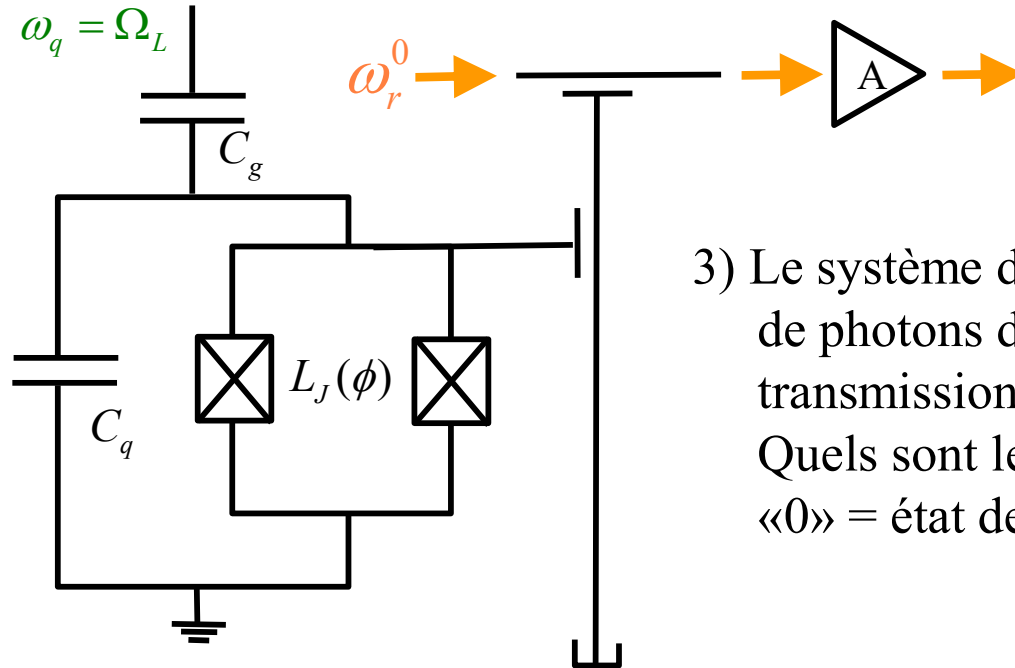
Au temps $t=0$, le qubit est dans l'état de base,
 Nous appliquons en continu un signal d'excitation à la fréquence
 de Larmor correspondant à la résonance du qubit ($\omega_q = \Omega_L$).
 Le qubit évolue à la fréquence de Rabi Ω_R .

2) Le système de mesure par non-démolition (excitation par injection
 de photons dans le résonateur et mesure électronique de la
 transmission) est enclenché à intervalles $\Omega_R.T = \pi/2$.

Quels sont les signaux détectés ?

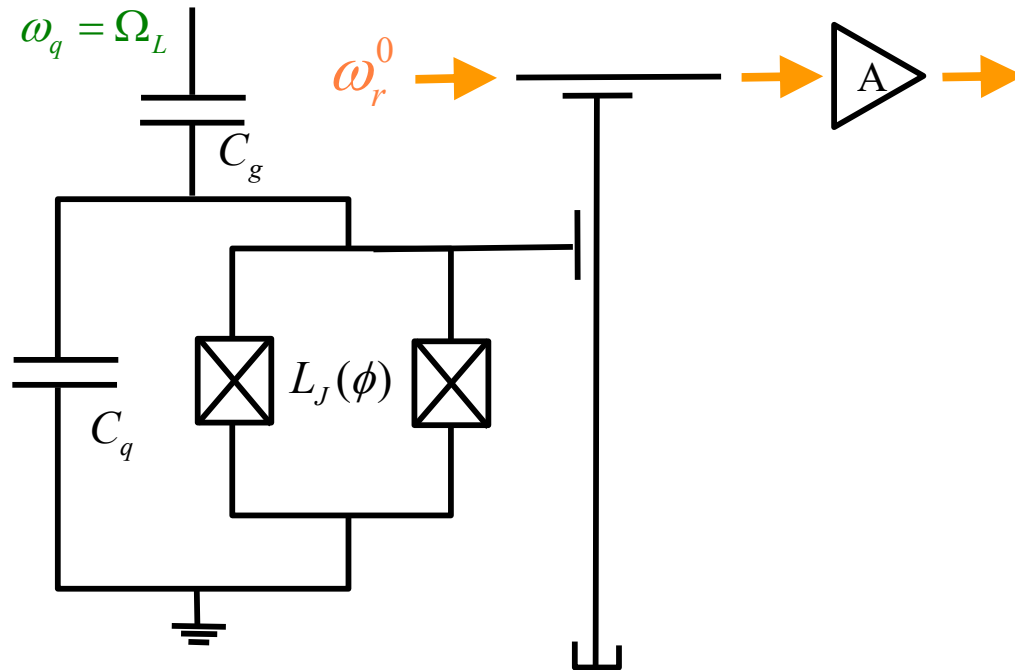
«0» = état de base, «1» = état excité

Exercice 13.2: effet Zénon



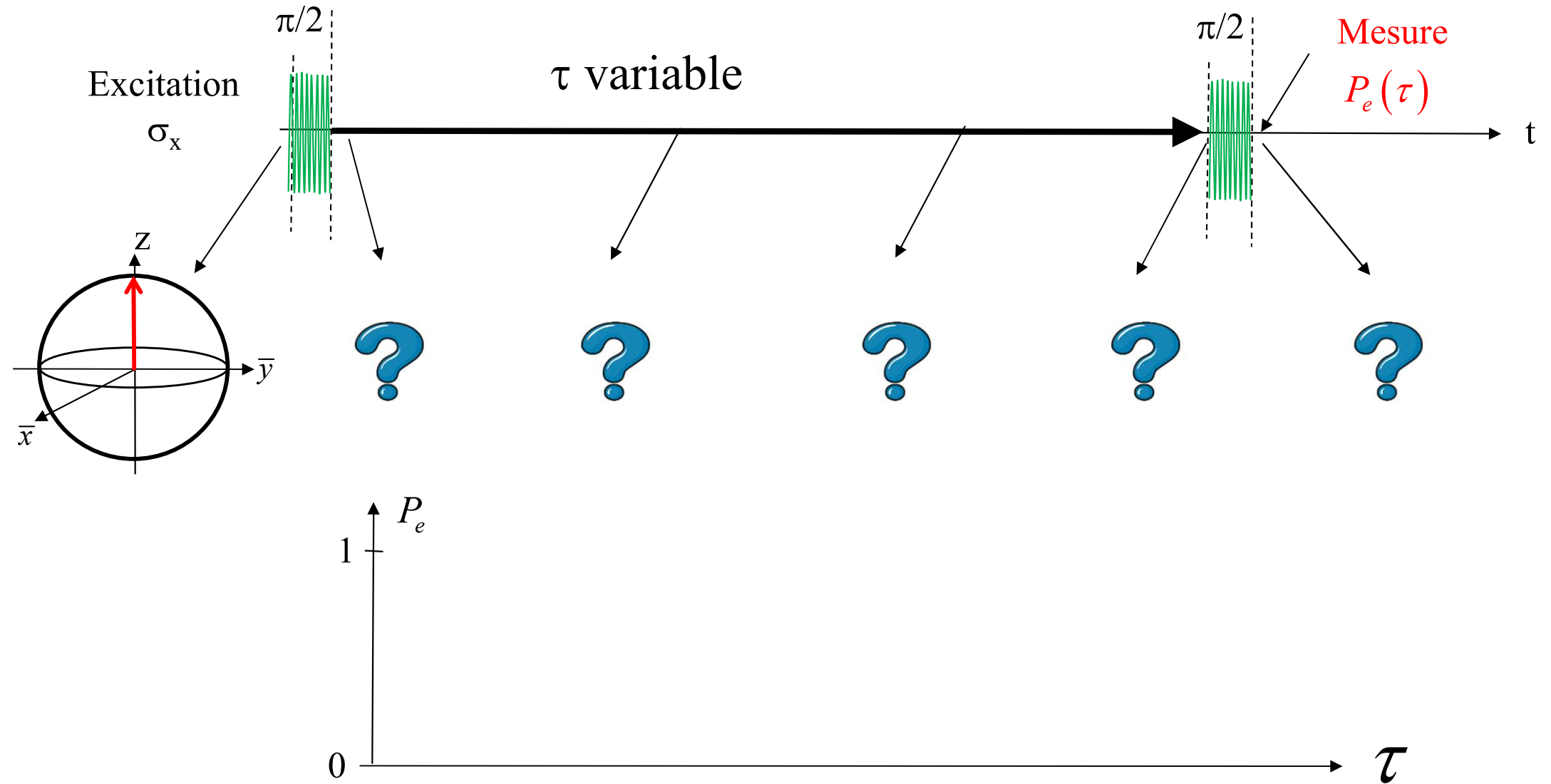
- 3) Le système de mesure par non-démolition (excitation par injection de photons dans le résonateur et mesure électronique de la transmission) fonctionne en continu.
Quels sont les signaux détectés ?
«0» = état de base, «1» = état excité

Exercice 13.2: effet Zénon

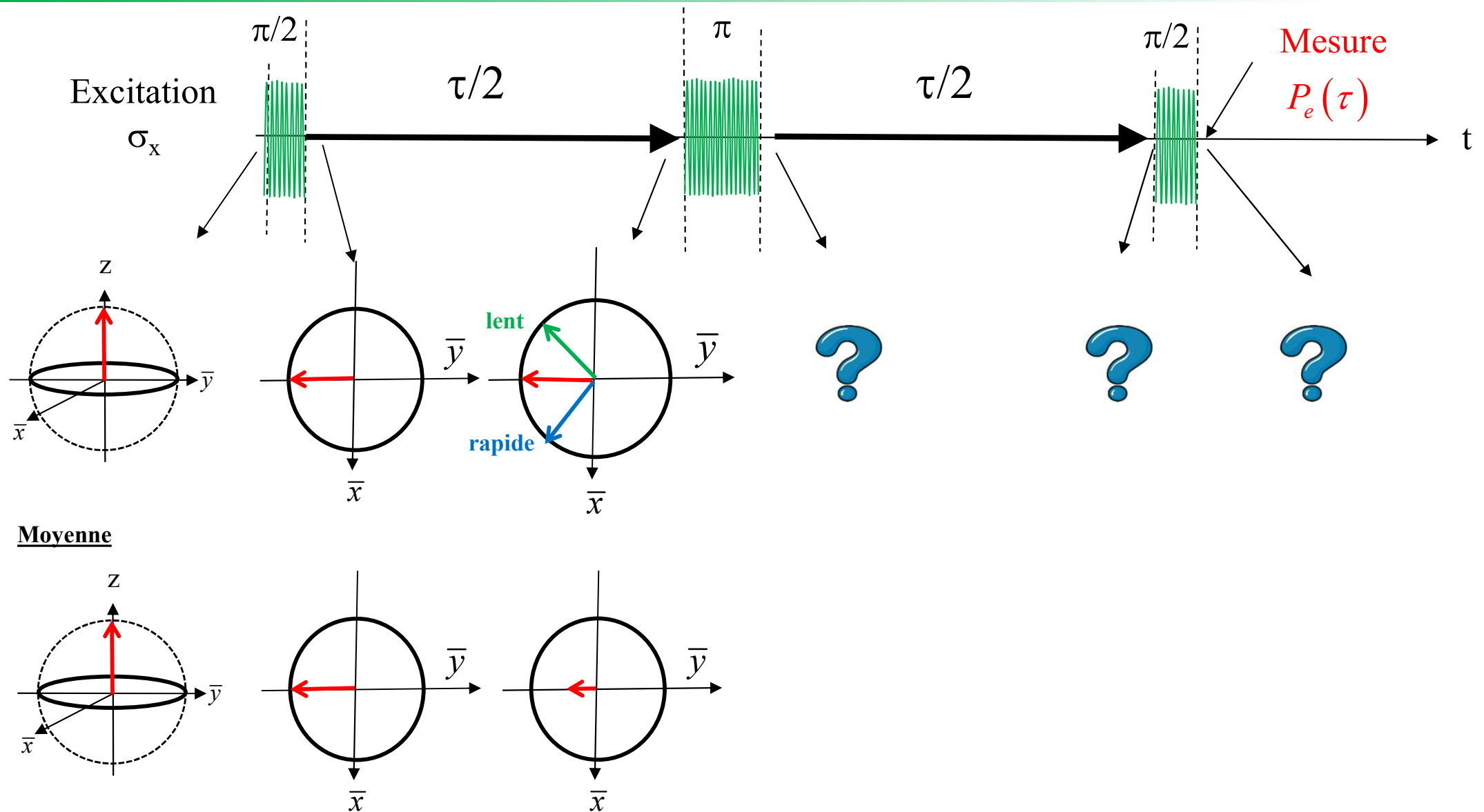


- 4) Seule l'excitation par injection de photons fonctionne en continu. La mesure électronique de la transmission est elle enclenché à intervalles $\Omega_R.T=\pi$
 Quels sont les signaux détectés ?
 «0» = état de base, «1» = état excité

Exercice 13.3 Mesures de décohérence: analysez ce cas, mesure de T_2^*



Exercice 13.4: Mesures de décohérence: analysez ce cas: mesure de T2



Exercice 13.4: Mesures de décohérence: analysez ce cas: mesure de T2

